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# Method for Classification of Snowflakes Based on Images by a Multi-Angle Snowflake Camera Using Convolutional Neural Networks

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## ABSTRACT

Taking advantage of the recent developments in machine learning, we propose an approach to automatic winter hydrometeor classification based on utilization of convolutional neural networks (CNNs). We describe the development, implementation, and evaluation of a method and tool for classification of snowflakes based on geometric characteristics and riming degree, respectively, obtained using CNNs from high-resolution images by a Multi-Angle Snowflake Camera (MASC). These networks are optimal for image classification of winter precipitation particles due to their high accuracy, computational efficiency, automatic feature extraction, and application versatility. They require little initial preparation, enable the use of smaller training sets through transfer learning techniques, come with large supporting communities and a wealth of resources available, and can be applied and operated by non-experts. We illustrate both the ease of implementation and the usefulness of operation the CNN architecture offers as a tool for researchers and practitioners utilizing in-situ optical observational devices. A training data set containing 1,450 MASC images is developed primarily from two storm events in December 2014 and February 2015 in Greeley, Colorado, by visual inspection of recognizable snowflake geometries. Defined geometric classes are aggregate, columnar crystal, planar crystal, small particle, and graupel. The CNN trained on this data set achieves a mean accuracy of 93.4% and displays excellent generalization (ability to classify new data). In addition, a separate training data set is developed sorting snowflakes into three classes showcasing distinct degrees of riming. The CNN riming degree estimator yields promising initial results but would benefit from larger training sets.

## 36 **1. Introduction**

37           The advent of dual polarimetric radar for weather observation and research has increased  
38 our capabilities to access and log vital data points within a given weather event. With excellent  
39 temporal and spatial resolution, researchers can accurately characterize shapes of the  
40 hydrometeors that compose a storm (Straka et al. 2000). Polarimetric radars provide the  
41 horizontal reflectivity,  $Z_h$ , differential reflectivity,  $Z_{dr}$ , and correlation coefficient,  $\rho_{hv}$ , of a  
42 field the radar is directed toward. This information gives insight to shape and type of  
43 hydrometeors within a storm and is calculated based on models developed by past observations.  
44 Scattering models fall short when left to spheroid approximations for frozen hydrometeors  
45 (Tyynelä et al. 2011). This is especially true at higher frequencies or for larger particles (Kim  
46 2006), and increases the need for accurate accounting of the varying microphysical  
47 characteristics of snow within a storm. Atmospheric scientists have drawn strong correlation  
48 between the environmental conditions present and the shape snow takes as it forms within a  
49 storm (Libbrecht 2017). Conditions within a storm are not homogenous, resulting in a wide  
50 variety of shapes that continue to change on the hydrometeor's path to the ground. While  
51 polarimetric radar provides excellent coverage, utilizing ground based (in-situ) devices in tandem  
52 with radar has proven more effective in understanding storm composition (Zhang et al. 2011),  
53 especially in studying riming degree. Riming (the collection of supercooled water droplets onto  
54 an ice crystals surface) is one of the physical metrics that can indicate valuable information about  
55 the internal characteristics of a storm and is of significant interest to the atmospheric science  
56 community (e.g., Kennedy et al. 2018). In-situ devices are often deployed on the ground in the  
57 path of a storm and allow for detailed sampling utilizing high resolution imaging techniques to  
58 capture individual hydrometeors while monitoring local environmental conditions (e.g.,

59 temperature, humidity, and wind speed). Some examples of in-situ image capturing devices  
60 include the Two-Dimensional Video Disdrometer (2DVD; Schönhuber et al. 2008) or the  
61 Precipitation Instrument Package (PIP; a more advanced version of the Snow Video Imager  
62 described in Newman et al. 2009). Another such in-situ device developed specifically to sample  
63 snowflakes in free fall is the Multi-Angle Snowflake Camera (MASC). The MASC can capture  
64 high resolution images of individual snowflakes, which provides researchers an avenue to study  
65 the microphysical characteristics and make statistical predictions concerning a storm's  
66 composition. A deployed MASC is capable of capturing thousands of images an hour, and with  
67 typical storms lasting several hours, a fast, accurate and automatic method to organize and  
68 process image data based on shared characteristics is crucial to increased understanding. There  
69 exist several classification algorithms known to atmospheric research communities (e.g.,  
70 Chandrasekar et al. 2013; Besic et al. 2016) but they are limited to large swaths of a storm and  
71 not local sampled images. Developing a classifier that functions automatically on a per  
72 snowflake basis would be a critical first step in introducing intelligent post-storm processing  
73 capabilities to in-situ devices, reducing data processing time for research, and allowing devices  
74 to remain in the field for longer periods.

75 Machine learning algorithms have made huge strides in the past decade (Minar and  
76 Naher 2018), especially with classification tasks, and have a massive community invested in  
77 improving and expanding existing algorithms. Previous attempts have been made to apply  
78 machine learning to snowflake classification with varying degrees of success. Early  
79 backpropagation neural networks (BPNNs) were used by Feind (2006) and multinomial logistic  
80 regression (MLR) by Praz et al. (2017). Feind (2006) achieved their best results using BPNNs  
81 with 85% accuracy in classifying eight categories of hydrometeors (drops, snow, hail, columns,

82 needles, plates, dendrites, and holes). Data was extracted using a PMS 2D-C probe that creates  
83 detailed particle profiles and is mounted on a T-28 aircraft which flies directly through storms.  
84 The images from the PMS 2D-C do not allow for microphysical characteristics of the particles to  
85 be considered, as the data is black and white profiles. Praz et al. (2017) set the standard for  
86 expert research into hydrometeor classification with a separate algorithm for feature extraction  
87 and optimization, and achieved a classification accuracy of 95%. Due to the high-resolution  
88 images used as their sample data, they can consider particle microphysical characteristics, as  
89 well as make estimations regarding degree of riming present. On the other hand, their algorithm  
90 requires external feature extraction and optimization, a process that may limit input complexity  
91 and number of classes due to the computational inefficiencies within the architecture. The feature  
92 extraction process would also need to be repeated with any hardware change as they likely  
93 incorporate hardware bias (imperfections unique to the device) into a data set, thus reducing the  
94 generality and versatility of the method.

95         This paper takes advantage of the most recent developments in machine learning and  
96 proposes an approach to automatic winter hydrometeor classification based on utilization of  
97 convolutional neural networks (CNNs). It presents the development, implementation, and  
98 evaluation of a CNN-based method and tool for classification of snowflakes using high-  
99 resolution images by a Multi-Angle Snowflake Camera. Snowflake classifications based on  
100 geometric characteristics and riming degree, respectively, are described and tested.  
101 Convolutional neural networks by their nature and properties are an excellent candidate for an  
102 algorithm and tool for classification of hydrometeors (and particularly winter precipitation)  
103 based on high-resolution images of particles. They were developed with image processing in  
104 mind, which makes them computationally more efficient for image-based classification when

105 compared to other multilayer backpropagation neural networks. CNNs act as a sort of “black  
106 box”, which automatically extract features during training, thus simplifying any system they are  
107 integrated into, with interest in data specific metrics available through further processing. CNNs  
108 can store these features, which increases their versatility as they are capable of transferring  
109 learning from one data set to another and are not limited to specific parameters inherent either to  
110 the data set (e.g., resolution, color, or size) or capturing method (e.g., hardware imperfections  
111 reflected in data). Therefore, a classifier properly trained with a CNN can be utilized by a variety  
112 of image-capturing in-situ devices. Research into deep learning has extended their ability to  
113 process complex data without major changes to the algorithm. Finally, CNNs are well  
114 understood algorithms that are extremely popular for image processing with a wealth of  
115 resources available, thus reducing a reliance on expert help in implementation (Mathworks  
116 2018a, 2018b).

117 In this paper, the steps needed to develop a hydrometeor classifier using CNNs are  
118 presented in detail and advantages to in-situ research are highlighted. The intention of this work  
119 is to illustrate the ease of implementation the CNN architecture offers as a tool for researchers  
120 and practitioners utilizing in-situ measurement devices. The CNN method described here  
121 requires less training data [e.g., 1,450 training samples, compared to 2,000 used by Fiend (2006)  
122 or 3,000 used by Praz et al. (2017)], as well as less image preprocessing, while attaining a  
123 geometric classification accuracy of 93.4%, for instance, which is comparable to other  
124 classifiers. Moreover, the new method provides extra flexibility for expanded functionality (e.g.,  
125 additional classes, different hydrometeor types, etc.) that can readily and non-expertly be  
126 achieved as the backend of a deployed measurement device and frontend to further data  
127 processing and analyses. Data preprocessing is reduced to cropping images to remove instances

128 where multiple snowflakes are present and a brightness thresholding filter to remove images  
129 which are too dim or blurry. Both steps are handled by a simple script which can then feed the  
130 processed images directly to each classifier. The classifier then organizes the data based on  
131 image features and places data in folders labeled for each class. This process is fast and  
132 computationally efficient; for example, the tool can be deployed in computers typically running  
133 in-situ measurement devices. The classifier in this work is developed using MATLAB™ 2018,  
134 but open-source toolboxes are available if additional flexibility is required.

135

## 136 **2. Snowflake Data Collection and Preparation**

137 This section describes how and under what conditions data was collected. Steps required  
138 in preprocessing of image data are covered. The classification criteria for geometric shapes and  
139 riming degree estimation are discussed.

140

### 141 **2.1 Data Collection Site**

142 The images that compose the training set were taken primarily from two winter weather  
143 events using a modified MASC system located at a surface instrumentation field site that was  
144 established as part of MASCRAD (MASC + RADar) project (Notaroš et al 2016; Bringi et al.  
145 2017; Kennedy et al. 2018). The MASCRAD field site, Figure 1, is located at the Easton Valley  
146 View Airport, in La Salle, outside of Greeley, Colorado. This site includes a modified MASC  
147 system, a 2DVD, a PLUVIO all-weather precipitation gauge, and a VAISALA weather station,  
148 amongst other advanced in-situ measurement instruments. These devices are situated within a  
149 double fence intercomparison reference (DFIR) and operate under the umbrella of the CSU-  
150 CHILL Radar, a state-of-the-art polarimetric weather radar located 12.92 km away.

151           The image data was collected during two events in the 2014-2015 deployment season of  
152 the MASCRAD project. The first took place from December 23<sup>rd</sup> to 31<sup>st</sup> in 2014, with the highest  
153 density of particles falling during the early morning hours of December 26<sup>th</sup>. To include enough  
154 graupel images, a second weather event was required (Bang et al. 2016). This event took place  
155 on February 21<sup>st</sup> – 22<sup>nd</sup> in 2015.

156

## 157 **2.2 Data Collection Device**

158           The Multi-Angle Snowflake Camera, or MASC, is the centerpiece of the MASCRAD  
159 project. While the finer details of the system are provided in (Garrett et al. 2012), for the  
160 purposes of this study a summary and brief description follows. The original MASC system is an  
161 instrument used to capture high-resolution images and fall speeds of hydrometeors in freefall  
162 from three different coplanar perspectives. These cameras are 5 Megapixel (MP) Unibrain Fire-I  
163 980b digital cameras with identical 12.5-mm Fujinon lenses. The cameras are spaced on a  
164 horizontal ring with 36° separation between adjacent cameras, with camera-to-common focal  
165 center distances of 10 cm. The system used at Colorado State University, Figure 2, has been  
166 modified to include two additional cameras at an elevated angle of 55° above the horizon. These  
167 are 1.2 MP Unibrain Fire-I 785b cameras with 12.5-mm lenses, included to improve the 3D  
168 virtual reconstruction using the visual hull method (Kleinkort et al. 2017). The system has a  
169 horizontal resolution of 35 μm for the three horizontal cameras and a vertical resolution of 40  
170 μm at 1-m/s fall speed. As hydrometeors fall through the horizontal ring, a near-IR emitter-  
171 detector pair sensor array (located on the top rim of the capture volume within the ring)  
172 simultaneously triggers the cameras and a flash (LEDs). The cameras have a maximum  
173 triggering rate of 2 Hz, a hardware limitation within the cameras, not set by the emitter-sensor



174 pair array. Finally, measurement of the time between upper and lower near-IR emitter-sensor  
175 triggers by a particle is used to calculate the particle fall speed (which is not the topic of this  
176 work).

177

## 178 **2.3 Image Preprocessing**

179 As a CNN automatically extracts features (numerical descriptors common between  
180 classes) during training that are to be used in classification, the image data base requires minimal  
181 preprocessing. A simple brightness thresholding is utilized to remove the majority of blank, dim  
182 or blurry images. Generally, a MASC is deployed during storming conditions, those with heavy  
183 wind or flurried snow, which can (in spite of the DFIR) cause the MASC to trigger without a  
184 snowflake in the focal area, making the need for thresholding crucial to processing. After  
185 thresholding to remove poor quality images, the creation of a training set requires a one-to-one  
186 correlation between an image of a snowflake and the class the image is being assigned to, i.e.,  
187 there can only be one snowflake per image. The task of separating images was automatically  
188 performed using a cropping script developed to find the brightest point of an image, locate the  
189 surrounding edges through their calculated standard deviations, and remove the snowflake to be  
190 saved in another location. The script then performs this action again until all independent bright  
191 spots have been cropped in a given image. This procedure is not perfect (<10% of snowflakes  
192 need repairs) but is dramatically more efficient than cropping images by hand.

193

## 194 **3. Hydrometeor Classification Scheme and Training Sets**

195 With machine learning algorithms, there are two categories of how learning is conducted:  
196 supervised or unsupervised. CNNs are supervised learning algorithms, therefore they require the

197 development of a labeled data set, referred to as the training set. This training set allows a human  
198 operator to dictate how the network makes decisions, by providing desired data for the network  
199 to make comparisons against. This contrasts unsupervised learning, where a network runs until it  
200 converges on a pattern or an end condition is reached. As expected, supervised learning is more  
201 efficient but does require additional setup in the development of the learning set and may be  
202 subject the supervisor's bias in selecting representative data.

203         The training set is developed by human inspection following a predetermined  
204 classification scheme. The idiom is that every snowflake is unique, therefore it is no surprise that  
205 there are a variety of attempts to classify them (Korolev and Sussman 2000, Grazioli et al. 2014),  
206 with little commonality between schemes. The scheme used in this work was adopted from Praz  
207 et al. (2017), who developed a snowflake classifier using Multinomial Logistic Regression  
208 (MLR) and will be summarized in this section.

209         The scheme utilizes the nine categories of snowflakes detailed in (Magono and Lee  
210 1966), with some changes due to data availability and simplification. They introduce the  
211 category of Aggregate particles, which are single snowflakes that are the result of the in-air  
212 collision of two or more particles and Small Particles, snowflakes whose feature characteristics  
213 are too small to categorize. They also combine the category of needle and column type  
214 snowflakes, as they share similar characteristics. Their result was 10 individual categories that  
215 include Aggregate (AG), Small Particle (SP), Columnar Crystal (CC; the resulting combination  
216 of needle and column particulates), Planar Crystal (PC), a Combination of Columnar Crystals, a  
217 Combination of Planar Crystals, Combination of Columnar and Planar Crystals, Graupel (GR),  
218 Irregular Snow Crystal, and Germ of Snow. Due to limited sample representation, the training set  
219 used in this paper includes only the most populated five classes, AG, CC, PC, SP, and GR,

220 shown in Figure 3, although more classes may be added to the classifier as sample data is  
221 accrued. A different training set is used for each classifier, and therefore their development  
222 considerations are unique to each set.

223

### 224 **3.1 Geometric Training Set**

225 At the heart of supervised learning is the comparison between the desired value  
226 (established in the training set) and a value calculated by the network, that is later refined  
227 through the learning process. This is an oversimplification, with more in-depth analysis provided  
228 in Section 4, but it is important to understand that the more unique the classes within a training  
229 set are from each other, the better the network will perform, given a limited training set (which  
230 seems obvious but cannot be overstated). The training set for geometric classification was  
231 developed by selecting individual images of the snowflakes that best represented their respective  
232 classes, with decision emphasis placed on discernable snowflake silhouettes. The result is a  
233 training set of ~1,450 samples.

234

### 235 **3.2 Riming Degree Estimation Training Set**

236 Riming degree estimations attempt to calculate the amount of cloud frozen droplets that  
237 accrue on a snowflake's surface as the snowflake falls through the atmosphere. The MASC  
238 system captures images with sufficiently detailed resolution that the degree of riming can be  
239 considered a feature of the image. There are two approaches to riming degree estimation  
240 considered in this paper. The first approach divides riming degree into 5 classes utilizing the  
241 classification scheme adapted by Praz et al. (2017). The second approach is a proposal that  
242 capitalizes on the unique nature of CNNs and warrants further exploration.

243 Praz et al. (2017) classify riming degree based on the image criteria summarized in Table  
244 1. These five degrees of riming,  $R_d$ , are discrete classes between [1,5] as developed by  
245 (Mosimann et al. 1994) and are then mapped by Praz et al. (2017) to a continuous index,  $R_c$ ,  
246 between [0,1], using a sinusoidal function:

$$247 \quad R_c = \frac{1}{2} \left( \sin \left( \frac{\pi}{4} (R_d - 3) \right) + 1 \right). \quad (1)$$

248 The degree label decisions are based on educated opinion through the observation of a  
249 captured image. Questions arise when pondering the level of accuracy that a human observer can  
250 achieve in their estimation. For example, the difference between a riming degree estimation of  
251 3.1 and 3.2 is often arbitrary and a matter of opinion or even capability. To address this concern,  
252 it is proposed to utilize the posterior distribution (a result of the classifier) that a CNN uses to  
253 make classification decisions as the deciding factor in riming degree estimation. The posterior  
254 distribution is a numerical value the classifier assigns to each snowflake describing the  
255 probability that it belongs to a given class or label. If labels are restricted to discrete values, the  
256 probability can be interpreted as the likelihood that a snowflake falls somewhere on that scale,  
257 making a continuous estimation.

258 Developing the training set for this approach, the classification scheme focuses on the  
259 three easily identified classes for riming estimation, then allows the network to assign probability  
260 estimations (clarified at the end of Section 4.2) for how closely a snowflake resembles those  
261 classes, labeled  $R_{l,c}$  and characterized in Table 1. The estimate training classes are class 1, where  
262 snowflakes are the least rimed (no riming present), class 3, where a snowflake is rimed but  
263 geometric shape is preserved, and class 5, where the snowflake is fully rimed (graupel). This  
264 simplifies the classification process and increases the consistency in decision making when  
265 applying labels while developing the training set. The result after classification is snowflakes that

266 do not fall directly within these three classes are weighted somewhere between. For example, if a  
267 snowflake's riming degree estimation is  $R_{l,c1} = 32\%$   $R_{l,c3} = 58\%$   $R_{l,c5} = 10\%$ , the estimation  
268 on Praz et al.'s (2017) scale is akin to  $\sim 2.78$ . The numerical values are used as an example, with  
269 a simple linear mapping. As more images are processed, a more accurate mapping can be  
270 developed if desired. This provides a continuous riming degree estimation and the opportunity  
271 for greater accuracy in estimation. Attention must be paid to the number of geometric classes  
272 represented in each riming category, as it is important to have uniform representation. This  
273 restriction limits the size of training set available, but the approach looks promising and will  
274 warrant further testing as processed data becomes available.

275

## 276 **4. Convolutional Neural Networks Method and Code**

277 A brief discussion of the network architecture is presented in this section. An overview of  
278 key concepts pertaining to CNNs and deep learning is provided. The software implementation  
279 and input parameters outlined before results of the network training are discussed.

280

### 281 **4.1 Neural Network Architecture**

282 A human brain can process information very quickly, namely, it has an ability to rapidly  
283 take incoming information, assign meaning, and make decisions. This is accomplished through a  
284 complex interconnected system of neurons that process information in parallel. It is no surprise  
285 then that considerable effort has been made to mimic the complex way the brain processes  
286 information with machine learning algorithms.

287 With artificial neural networks, more commonly known as "neural networks," the basic  
288 architecture of the brain is recreated in a logical algorithm. The basis for the network architecture

289 used in this paper is called the “Multi-Layer Perceptron (MLP),” which is a feed forward neural  
 290 network with backpropagation, whose general structure is represented in Figure 4a, and as an  
 291 algorithm in Figure 4b. In general, there is an input signal which is passed to the hidden layers  
 292 for processing, with final decision making the result of the output layer. The algorithm is “feed  
 293 forward” in reference to the direction of information and the “backpropagation” describes the  
 294 learning process, which is detailed below.

295 Referring to Figure 4b, the forward pass of the learning algorithm applies the input value  
 296  $x_{1...N}$  of training sample  $p$  with a weighted bias of  $w_{kj}^{(1)}(p)$ . This bias serves to both connect the  
 297 input  $j$  to neuron  $k$  and to refine the error estimation of the classifier,  $E_p$ , and are generally  
 298 random values between a range loosely defined by the number of inputs (Azimi 2018). The  
 299 potential of neuron  $k$  is represented by

$$300 \quad u_k^{(1)}(p) = \sum_{j=1}^{N+1} w_{kj}^{(1)}(p)x_j(p), \quad \forall k \in [1, K]. \quad (2)$$

301 The nonlinear activation function is, commonly, the logistic function  $f(\cdot)$  (Murphy 2012) or,  
 302 more recently (and in the case of this paper), the Rectified Linear Unit (ReLU),

$$303 \quad f(u) = \frac{1}{1+\exp(-u)} \quad \text{or} \quad ReLU(u) = \max(0, u). \quad (3)$$

304 This activation function determines the output of the current neuron, which, in turn, becomes the  
 305 input of the next layer within the network,

$$306 \quad o_k^{(1)}(p) = f\left(u_k^{(1)}(p)\right), \quad \forall k \in [1, K]. \quad (4)$$

307 This process is repeated until the final layer of the network is reached, labeled “Output” in  
 308 Figure 4b. It is at this point that the sum squared error of the classifier can be calculated,

$$309 \quad E_p = \frac{1}{2} \sum_{m=1}^M \left( d_m^{(output)}(p) - o_m^{output}(p) \right)^2. \quad (5)$$

310 Our goal is to minimize  $E_p$ , such that the desired output,  $d_m^{(output)}(p)$ , is as close to the  
 311 calculated output,  $o_m^{output}(p)$ , as possible. It is unlikely that  $E_p$  is within acceptable parameters  
 312 on the first pass of learning, therefore there needs to be some method to refine the weights to  
 313 approach convergence. This requires calculation of the partial derivative of  $E_p$  with respect to the  
 314 weight in the final layer, namely,  $w_{ml}^{(output)}$  in Figure 4b. The full derivation falls outside the  
 315 scope of this paper but can be found in various forms in (Murphy 2012; Haykin 2009; Syozil et  
 316 al. 1997). The final result for this example three-layer network is

$$317 \quad \Delta w_{ml}^{(output)}(p) = -\mu \nabla E_p(p) = \mu e_m^{output}(p) f' \left( u_m^{(output)}(p) \right) o_l^{H-1}(p),$$

$$318 \quad \forall m \in [1, M] \text{ and } \forall l \in [1, L], \quad (6)$$

319 where

$$320 \quad e_m^{output}(p) = d_m^{(output)}(p) - o_m^{output}(p), \quad \mu = \text{learning factor}. \quad (7)$$

321 Repeating this derivation for weight updates within the hidden layers shows that the calculated  
 322 layer from the output is back-propagated through the network,

$$323 \quad \Delta w_{ml}^{(output)} = \mu e_m^{output}(p) f' \left( u_m^{(output)}(p) \right) o_l^{H-1}(p), \quad (8)$$

$$324 \quad \Delta w_{ml}^{(output)} = w_{ml}^{(output)}(p+1) - w_{ml}^{(output)}(p), \quad \forall m \in [1, M], \quad (9)$$

$$325 \quad \Delta w_{lk}^{(H-1)} = \mu f' \left( u_l^{(H-1)}(p) \right) o_k^1(p) \sum_{m=1}^M w_{ml}^{(output)}(p) e_m^{output}(p) f' \left( u_m^{(output)}(p) \right), \quad (10)$$

$$326 \quad \Delta w_{lk}^{(H-1)} = w_{lk}^{(H-1)}(p+1) - w_{lk}^{(H-1)}(p), \quad \forall l \in [1, L], \quad (11)$$

$$327 \quad \Delta w_{kj}^{(1)} = \mu f' \left( u_k^{(1)}(p) \right) x_j(p) \sum_{l=1}^L w_{lk}^{(H-1)}(p) f' \left( u_l^{(H-1)}(p) \right)$$

$$328 \quad * \left[ \sum_{m=1}^M w_{ml}^{(output)}(p) e_m^{output}(p) f' \left( u_m^{(output)}(p) \right) \right], \quad (12)$$

$$329 \quad \Delta w_{kj}^{(1)} = w_{kj}^{(1)}(p+1) - w_{kj}^{(1)}(p), \quad \forall k \in [1, K]. \quad (13)$$

330 This back and forth is continued until the error stops decreasing or an acceptable value is  
331 reached.

332

## 333 **4.2 Convolutional Neural Networks**

334 With image classification, the input value of  $x_{1...N}$  is a pixel of the image in the training  
335 set and this presents a major limitation to typical MLP architectures. Each input has an individual  
336 weight value per neuron in the network, so for even a moderately deep network (the number of  
337 hidden layers in the network refers to how deep a network is), the result is upwards of hundreds  
338 of thousands of weights that require refinement, or even millions for very high resolutions,  
339 making this computationally inefficient for modern practical purposes. CNNs solve many of the  
340 problems MLPs experience for image processing and have proven useful with other data types  
341 (e.g., Collobert and Weston 2008, O’Shea et al. 2016). A visual representation of the CNN  
342 architecture is shown in Figure 5.

343 The defining features of the CNN architecture are the inclusion of the convolution layer,  
344 a pooling layer, and the fully connected layer. The convolution operator introduces several  
345 advantages to the architecture, namely sparse interactions, parameter sharing and equivariance to  
346 translation (Goodfellow et al. 2016). As is depicted in Figure 5, the convolution layer creates a  
347 series of feature maps by scanning a weight matrix of size  $[i,j]$  over the surface of the input data.  
348 This reduces the number of parameters the network must consider and introduces weight sharing.  
349 Comparing to Figure 4b, the inputs are blocked or shared between units with shared weights. The  
350 result is a reduction in memory requirements and an improvement of statistical efficiency  
351 (Goodfellow et al. 2016). After the convolution is performed, the linear activations that result are  
352 then passed through a nonlinear activation function, like the ReLU which has largely replaced



353 other activation functions, as it improves efficiency without a reduction in accuracy (Goodfellow  
 354 et al. 2016). The convolution layer can be repeated with different sized weight matrices to extract  
 355 more and more abstract features. LeCun et al. (1998) introduced the pooling, or subsampling,  
 356 layer to their model **LeNet5** to achieve shift invariance (Murphy 2012). This is accomplished by  
 357 either averaging or producing a max over a small window of the convolution layer. This step is  
 358 especially vital for image classification, as it allows the network to extract features without  
 359 concerning exactly where the features are located (Goodfellow et al. 2016). An additional benefit  
 360 of this property is that it makes transfer learning with pretrained networks possible (Torrey and  
 361 Shavlik 2009), which significantly reduces the size of training set necessary for new  
 362 classification schemes. **LeNet5** followed every convolution with a pooling layer, but this is  
 363 unnecessary. It has been shown that the best results for complex data sets apply a few pooling  
 364 layers after the first series of convolution layers and a final pooling layer after the next to last  
 365 convolution layer (Romanuke 2017). The final few layers of the network will consist of fully  
 366 connected layers which are akin to those in regular neural networks. The output of these layers  
 367 after activation are passed to a *softmax* operator  $\sigma(\cdot)$  where high-level decisions are made, and  
 368 after several passes, a class label is applied. The learning process is summarized as

$$369 \quad y_j = \sigma(\underline{z})_j = \frac{\exp(z_j)}{\sum_{k=1}^K \exp(z_k)}, \quad \forall j \in [1, K], \quad (10)$$

370 where  $y_j = p(C_j|\underline{x})$ , a posterior distribution over the available classes, with  $C_j$  standing for the  
 371 class and  $\underline{x}$  for the input vector. In Section 3.2, a term “likelihood” is used to provide a label to  
 372 the degree of riming present for a given snowflake, for added clarity,  $y_1 = R_{l,c1}$ ,  $y_3 = R_{l,c3}$ , and  
 373  $y_5 = R_{l,c5}$ . If  $\mathcal{W}$  is the set of all parameters for the network, and the set of training samples is  
 374  $\{\underline{x}_p, \underline{d}_p\}_{p=1}^P$ , then using  $y_j$  as an input to a cost function  $\varepsilon(\cdot)$ , whose minimization is achieved  
 375 through a modified error backpropagation (Azimi 2018),

376 
$$\varepsilon(\mathcal{W}) = \frac{1}{N} \sum_{p=1}^P \left\| \underline{d}_p - \underline{y}(\underline{x}_p; \mathcal{W}) \right\|^2. \quad (11)$$

377

### 378 **4.3 Residual Networks**

379 For complicated data sets, network comparisons have shown that increased depth  
380 improves network accuracy (Simonyan and Zisserman 2015, Szegedy et al. 2015). Deep  
381 networks have more capacity for different level (low/mid/high) features (Zeiler and Fergus  
382 2014), and the top performing networks on the ImageNet dataset have employed deep models  
383 (He et al. 2016). The tradeoff is that the deeper the network becomes, the more the accuracy  
384 saturates and begins to quickly decline (He et al. 2016). To combat this, a group of researchers  
385 from Microsoft Research, He et al. (2016), have utilized the residual network architecture. A  
386 residual network architecture is very similar to a convolutional neural network, with one  
387 addition. Namely, every few convolutional layers, a short cut identity is included, Figure 6,  
388 which fits the layers to a residual mapping, instead of hoping that they would come to a desired  
389 mapping naturally (He et al. 2016).

390

### 391 **4.4 Software Implementation**

392 A major benefit to utilizing convolutional neural networks for hydrometeor classification  
393 based on high-resolution images is their (recent) widespread popularity for image processing in  
394 general. As a result of this popularity and widespread use, there are extensive software toolboxes  
395 available, both commercial and open source, with detailed walkthroughs for a variety of tasks  
396 and applications. Due to the automatic feature extraction inherent to their algorithm, CNNs can  
397 be applied and operated by non-experts, increasing their functionality as a preprocessing

398 frontend for big data tasks. The toolboxes and setup utilized in this study are described as  
399 follows.

400         The same network architecture is used for geometric classification and riming degree  
401 estimation and can be run in parallel. The network was implemented using MATLAB™ 2018,  
402 with the Deep Learning and Machine Learning Toolboxes at Colorado State University. The  
403 network architecture is the **ResNet-50**, which was chosen over **AlexNet** (Krizheysky et al. 2012)  
404 or **GoogleNet** (Szegedy et al. 2015) due to its balance between accuracy and speed (Mathworks  
405 2018c) and has been pretrained on the ImageNet database (Russakovsky and Deng et al. 2015) to  
406 reduce the size of the training set data necessary to be an effective classifier. The more  
407 complicated the classification task, the larger the data set needed to extract relevant features (He  
408 et al. 2016). Geometric classification, however, is a common problem in image classification,  
409 and therefore it is an ideal candidate for pretraining. A network pretrained for image  
410 classification can reuse many of the features extracted and made task specific on a reduced  
411 training data set (del-Rio et al. 2018). Each class in the training set is limited to the smallest  
412 populated class, for instance, the Planar Crystal class is the least populated and has 290 images,  
413 this then sets an upper limit of 290 on all classes. This is done so overrepresentation does not  
414 occur in the training phase. The entire training data set is divided into two categories, “training”  
415 and “validation”. As is customary, 70% of the entire training data set is randomly selected and  
416 stored in the “training” category, with the remaining 30% saved for validation of the network  
417 performance. This separation reduces the likelihood of the network overfitting to data and allows  
418 for an accurate test for generalization. The training images are randomly reflected, translated and  
419 scaled within a defined range to improve the networks invariance to small changes (Murphy  
420 2012). A technique known as Dropout (Srivastava et al. 2014) is employed on the pretrained

421 network weights to further reduce any overfitting that may occur. The network performance is  
422 determined by mean square and the loss function is calculated as stochastic gradient descent.  
423 Validation occurs every three iterations over 10 epochs (one epoch is a training phase where all  
424 training data is considered), although experimentation has shown that 6 epochs are enough to  
425 improve training time without loss of performance as is adopted for later tests. The learning rate  
426 for both networks is 0.0003.

427

## 428 **5. Results and Discussion**

429 This section presents and discusses the results of the geometric classification and riming  
430 degree estimation using the described method for classification of snowflakes based on images  
431 by a multi-angle snowflake camera by means of convolutional neural networks. The learning  
432 curves for each network are presented, along with an associated confusion matrix calculated  
433 from blind data to highlight the network's generalization (the ability for a network to classify  
434 new data).

435

### 436 **5.1 Geometric Classification**

437 The results of network training for geometric classification are shown in Figure 7. The  
438 training data set included ~1,450 images and training occurred over 900 iterations. The network  
439 achieves a mean accuracy of 93.4% with a loss function of ~0.2 and little variance between runs.  
440 Training time was 13 minutes and 23 seconds. This is very good accuracy given the size of the  
441 data set and the training time is reduced when limited to 6 epochs (from ~13 min to ~8 min). To  
442 test the generalization of the network, it is then used to classify ~400 snowflakes not included in  
443 training, the results of which are shown in Figure 8.

444           The relevant information from the confusion matrix can be seen in the bottom row and  
445 right-most column. The bottom row is the percentage value of when the network was presented  
446 with an image and correctly classified it on a per class basis. The right-most column is out of  
447 class accuracy, i.e., how often the network confused an image within a class for something else.  
448 The confusion matrix shows that the network has some issues making decisions between planar  
449 crystal and aggregate snowflakes. This is consistent with established reasoning, as the planar  
450 crystal class is most visibly similar to aggregate snowflakes and was also the smallest  
451 represented class for training which limited the diversity of available samples. Increasing the  
452 number of samples should enhance the network’s ability to differentiate between the two classes.

453

## 454 **5.2 Riming Degree Estimation**

455           With riming degree estimation, two networks were trained for comparison. One of the  
456 networks keeps the discrete five classes determined using Praz et al’s (2017) [1,5] classification  
457 scheme (Table 1), while the other network removes the two classes labeled 2 and 4, relying  
458 instead on the posterior distribution, or “likelihood” estimation, to assign a continuous label to  
459 snowflakes that fall within the edge cases. Comparing the learning curves of the two networks  
460 (Figure 9), it is clear that classes 2 and 4 are difficult for the network to analyze. The result of  
461 training is a mean accuracy of 68.8% and a loss of ~1 for the network trained on five classes  
462 (Figure 7a) and a mean accuracy of 92.4% with a loss of <0.3 for the network with only three  
463 classes (Figure 7b). The second network is then tasked with classifying a data set that includes  
464 samples from all five classes. Results of the applied “likelihood” percentage,  $R_{l,c\#}$ , are shown in  
465 Figure 10. Here we show the network’s capability to apply a riming degree estimation  
466 determined by features found in the edge case classes used in training. In Figure 10, examples of

467 individual degree estimations are depicted in the top-most row, while the network’s capability to  
468 distinguish between snowflakes with similar characteristics is showcased on the bottom. An  
469 inherent benefit of this estimator is that it removes some of the guesswork involved when a  
470 human user classifies snowflakes individually. While the human processor may introduce error  
471 through fatigue or the result of an immediacy bias, a network will not suffer from these potential  
472 pitfalls and may catch misclassified images (Figure 11). Note that a larger, more diverse training  
473 data set will be required before more accurate and conclusive tests can be performed.

474         Developing a riming degree estimator relies almost entirely upon features that are unique  
475 to images of snowflakes. Best results will be derived from training sets where features unrelated  
476 to riming degree estimation are equally represented, so that they are effectively removed from  
477 the decision-making process. Without equal representation, the network can develop a bias based  
478 on which feature is more prevalent. An example of this bias shown in Figure 12 is a result of  
479 columnar crystal images being overrepresented in the “no riming” category. In Figure 12a, the  
480 estimator gives an accurate prediction indicated by the  $R_{l,c\#}$  values, but the bias is evident in  
481 snowflakes in Figures 12b and 12c, resulting in a severe underestimation and overestimation,  
482 respectively. In the storms sampled, snowflakes demonstrating no degree of riming were  
483 relatively rare, which is why columnar crystal snowflakes compose the bulk of the data set. To  
484 achieve equal representation of unrelated snowflake features, a wider variety of storms from  
485 different seasons will need to be processed.

486

## 487 **6. Conclusions**

488         This paper has applied recent developments in machine learning to the problem of  
489 automatic winter hydrometeor classification. Utilizing convolutional neural networks, the task of

490 classifying snowflakes based on geometric characteristics and riming degree has been  
491 undertaken. Convolutional neural networks are ideal for image classification due to their  
492 efficient data handling, automatic feature extraction, versatility, and relative ease of application.  
493 A training set has been developed primarily from two winter precipitation events and consists of  
494 1,450 snowflakes. Six geometric classes have been defined based on observable physical  
495 characteristics of the snowflakes. These classes are aggregate, columnar crystal, planar crystal,  
496 small particle, graupel, and a combination of columnar and planar (although the latter is  
497 discarded due to rarity until further data is processed). Geometric training has focused on  
498 individual snowflakes that are easily identifiable as members of a single class. The result of  
499 training is a network with 93.4% classification accuracy. This performance is sufficient to begin  
500 processing the many hours of recorded data from the MASCRAD project and begin growing the  
501 training data set for continued network development. Currently, our CNN is best equipped for  
502 small-batch processing (few hundred snowflakes per batch) due to the size of its training data set.  
503 By processing more data with diverse environmental conditions, the network will eventually be  
504 able to process bulk data that number in the thousands and tens of thousands, and more. With  
505 additional snowflake variety, geometric sub-classes and rarer classes may be introduced to the  
506 network, expanding from the five classes currently utilized.

507         The results obtained by the riming degree estimator using a CNN have shown promise.  
508 The training set is composed of images from all geometric classes separated (where applicable)  
509 into three categories: no riming, rimed, and graupel. The network has achieved 92% accuracy  
510 when estimating snowflakes that fall into these categories of riming. The probabilistic estimation  
511 that results at the output layer of the CNN has then been used to gauge where a snowflake falls  
512 within these three degrees of riming (classes 2 and 4 from Praz et al.). The high degree of

513 accuracy has been maintained by the network in determining whether a snowflake is more rimed  
514 or less rimed (belonging in class 2 or 4) but more sample data must be developed to increase  
515 precision of estimation and remove the influence of feature bias. Feature extraction requires a  
516 large number of images and features unique to snowflake images cannot be compensated for by  
517 pretraining on unrelated images. More diverse snowflakes will help remove any bias the network  
518 develops. For example, a method for mapping the estimation to fit Mosimann et al. (1994) can be  
519 developed as more output data becomes available. Finally, processing data from different  
520 seasons may lead to additional classification tasks, such as wet vs. dry snow, and may be  
521 considered in future applications of the CNN classification approach.

522         The classification network developed and presented in this paper will be used in the  
523 processing of MASCRAD data, but the architecture is suitable for any solid hydrometeor  
524 classification task and is suitable as a preprocessing frontend to any image-based particle  
525 recording instrument/device or system. The network is fitting for users with limited experience in  
526 image processing, machine learning or atmospheric research. Organized data by geometric and  
527 microphysical characteristics and accurate riming degree estimations will help further research  
528 into hydrometeor scattering. An example of future work is related to linking the microphysical  
529 characteristics of snowflakes to the scattering properties through 3D shape reconstruction and  
530 modeling (Kleinkort et al. 2017), followed by the realistic scattering computation (Chobanyan et  
531 al. 2015). Overall, this and many other applications of automatic CNN-based winter hydrometeor  
532 classification will potentially improve propagation models as higher frequencies continue to be  
533 explored, whether for use in remote sensing of hydrometeors, communication or other related  
534 fields.

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## 706 Tables

707 **Table 1.** Physical descriptions characterizing the degree of riming,  $R_d$ , on a given snowflake,  
 708 with numerical representations as described by Mosimann et al. (1994), in column 2. Column 1  
 709 contains degree estimations,  $R_c$ , utilized by Praz et al. (2017). Column 3 gives the probability  
 710 estimates,  $R_l$ , used in this paper.

$R_c$ $\in [0,1]$	$R_d$ $\in [1,5]$	$R_l \in [1,5]$	Coverage of the surface	Description
0	1 (none)	1.0 ( $R_{l,c1} \geq 99\%$ )	0%	No cloud droplets on the surface. Snowflakes are detailed and delicate in appearance.
0.15	2 (rimed)	to 2.99 ( $R_{l,c1}, R_{l,c3} > R_{l,5}$ )	$\simeq 50\%$	Up to half of the surface is covered with cloud droplets. There may be delicate features, but some clumping has occurred.



0.5	3 (densely rimed)	3.0 ( $R_{l,c3} \geq 99\%$ )	$\approx 100\%$	The entire snowflake is covered with cloud droplets, but the general shape is conserved.
0.85	4 (graupel-like)	3.01 to 4.99 ( $R_{l,c5}, R_{l,c3} > R_{l,c1}$ )	$> 100\%$	The entire snowflake is heavily covered with cloud droplets, to the point where the original shape is barely recognizable
1.0	5 (graupel)	5.0 ( $R_{l,c5} \geq 99\%$ )	$\gg 100\%$	The entire snowflake is heavily covered with cloud droplets. Original shape is no longer distinguishable and has entered the class of graupel.

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### Figure Caption List

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715 **Figure 1.** MASCRAD Snow Field Site at Easton Valley Airport, near Greeley, Colorado, under  
 716 the umbrella of CSU-CHILL Radar. MASC (top right), along with other surface instrumentation,  
 717 is contained in the 2/3-scaled DFIR.

718

719 **Figure 2.** Multi-Angle Snowflake Camera (MASC), with three cameras in the horizontal plane  
 720 for capturing high-resolution photographs of winter precipitation (top left); The CSU MASC  
 721 system has been modified to included two cameras situated on an elevated plane, poised at  $55^\circ$   
 722 above the horizon to aid in the visual hull 3D particle shape reconstruction (top right); Example  
 723 images from each camera, the first three columns are from the horizontal cameras and the final  
 724 two are from the lower-resolution raised cameras (bottom two rows, from left to right).

725

726 **Figure 3.** Examples of MASC images characterizing the geometric classes (top row) and riming  
 727 degree estimations (bottom row).

728

729 **Figure 4.** (a) Feed Forward Network architecture demonstrating how each neuron is connected  
730 to every neuron in the previous layer. (b) Algorithm for feed forward learning process within the  
731 network.

732

733 **Figure 5.** Highlighting the key steps within a typical convolutional neural network: The input  
734 layer is scanned with a  $[i,j]$  weight matrix to create the feature map; The feature map is averaged  
735 or maxed to increase network efficiency in the pooling layer; Decision making occurs at the final  
736 fully connected layer.

737

738 **Figure 6.** Additional Residual step introduced to a typical neural network architecture.

739

740 **Figure 7.** A mean average is validated every three iterations (black dots) over 10 epochs with a  
741 mean average of 93.4% (top), the same parameters are shared by the loss function evaluation  
742 with a final value of  $\sim 0.2$  (bottom).

743

744 **Figure 8.** The network was tasked with classifying 395 snowflakes to test generalization. The  
745 left axis is what the network labeled the input data as, and the bottom axis is what the input data  
746 was. Green boxes represent correctly classified images, with total number in bold and percentage  
747 of total immediately below. Green text represents a correct classification, while the red  
748 percentage is the misclassification of the network. The overall network accuracy is shown in the  
749 bottom right corner.

750

751 **Figure 9.** (a) A network was trained using classes composed of images representing the five  
752 discrete riming degree values [1,5] described in Table 1; (b) A separate network was trained  
753 using the same image data, only removing the images comprising classes 2 and 4.

754

755 **Figure 10.** The values represent the output of the riming degree estimation network: the top row  
756 highlights the network’s range, while the bottom mostly demonstrates its ability to differentiate  
757 between similar snowflakes.

758

759 **Figure 11.** Utilizing a neural network for riming degree estimation has the advantage of  
760 quantified data driven decision making.

761

762 **Figure 12.** (a) An image of a correctly labeled image by the Riming degree estimator. (b) The  
763 network underestimates the degree of riming in the image due to feature bias present in the “no  
764 riming” class. Expected results for this image should be a higher value for  $R_{l,c3}$ . (c) The network  
765 overestimates the degree of riming due to feature bias from the “graupel” class.

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## Figures

769

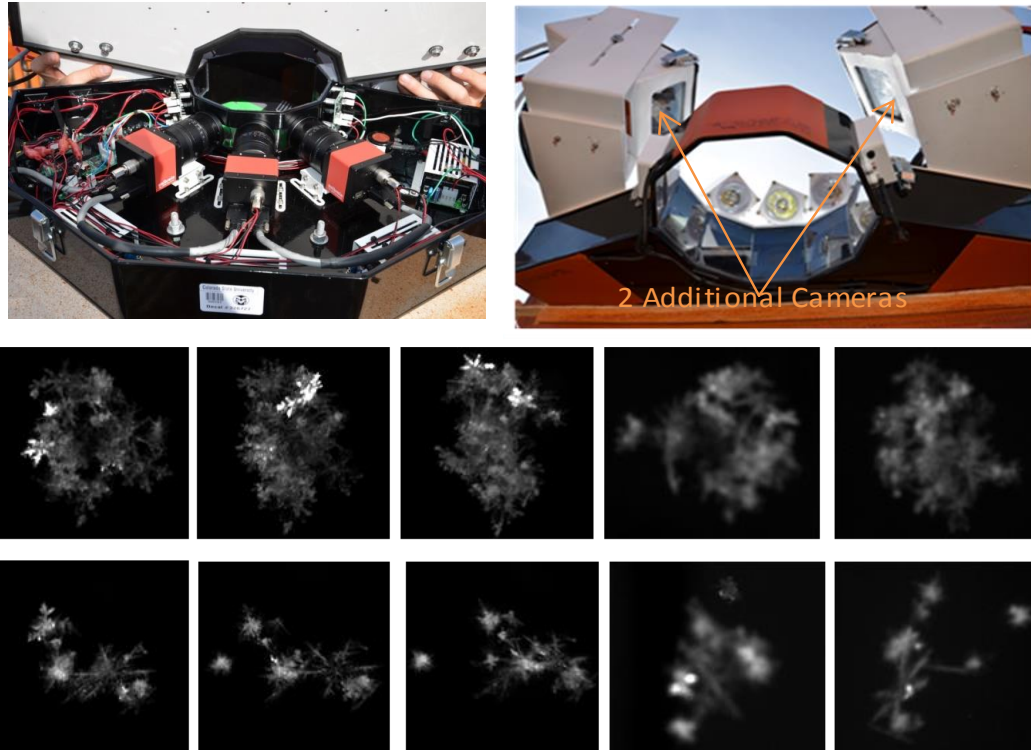


770

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772 the umbrella of CSU-CHILL Radar. MASC (top right), along with other surface instrumentation,  
773 is contained in the 2/3-scaled DFIR.

774

775

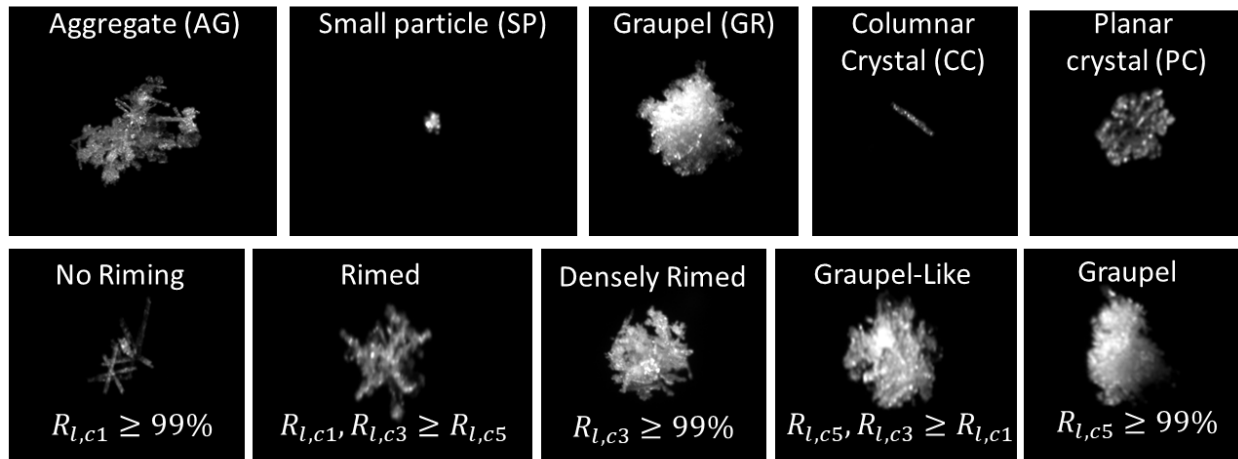


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781 images from each camera, the first three columns are from the horizontal cameras and the final  
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783

784



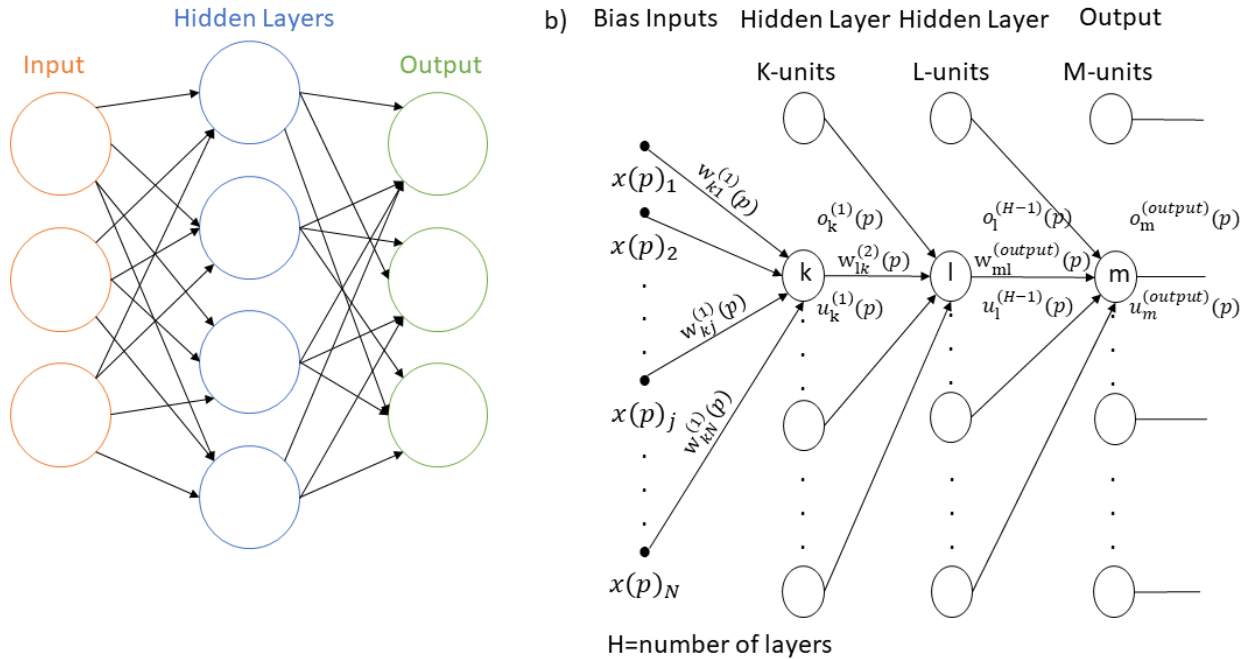
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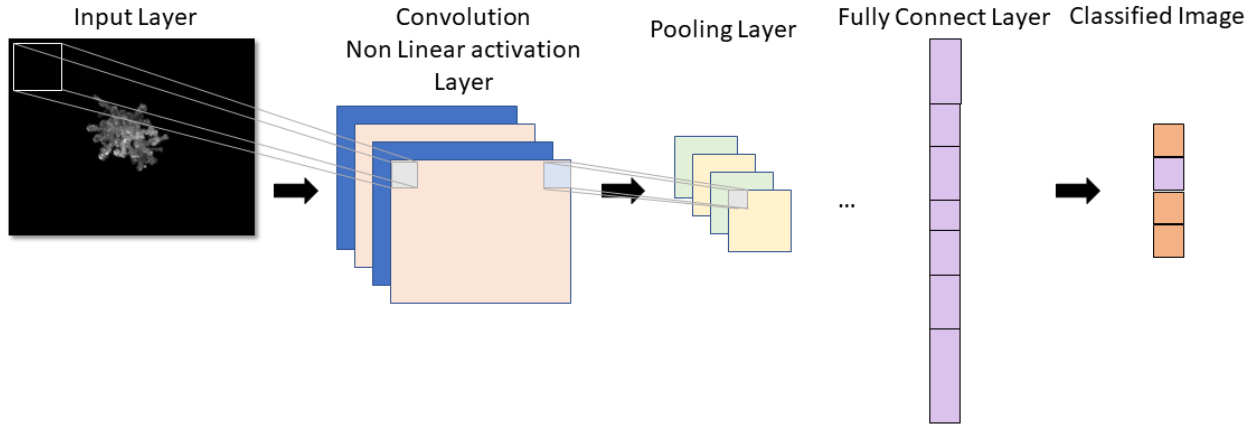
794

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798

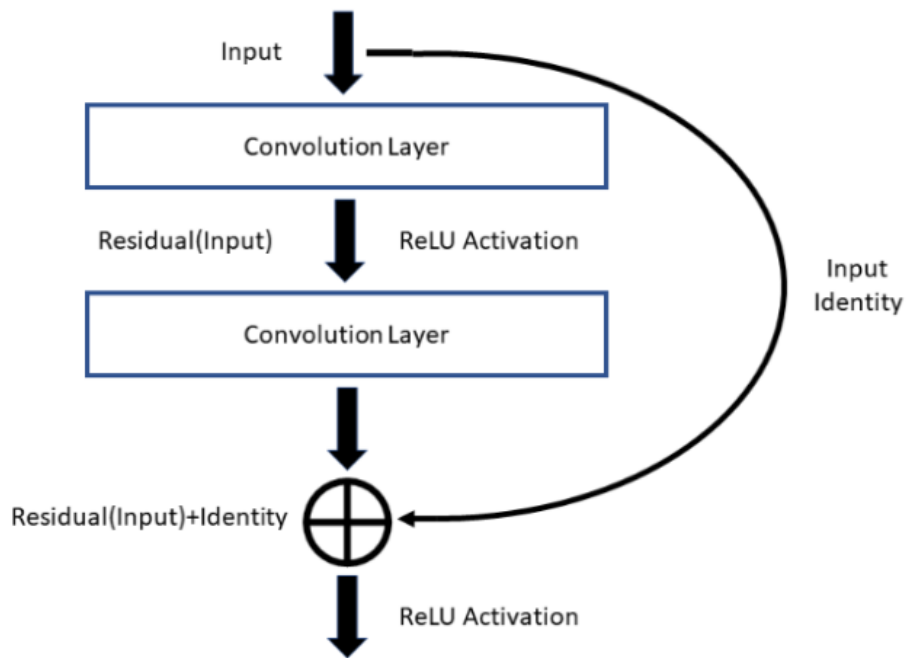


799

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 802 or maxed to increase network efficiency in the pooling layer; Decision making occurs at the final  
 803 fully connected layer.

804

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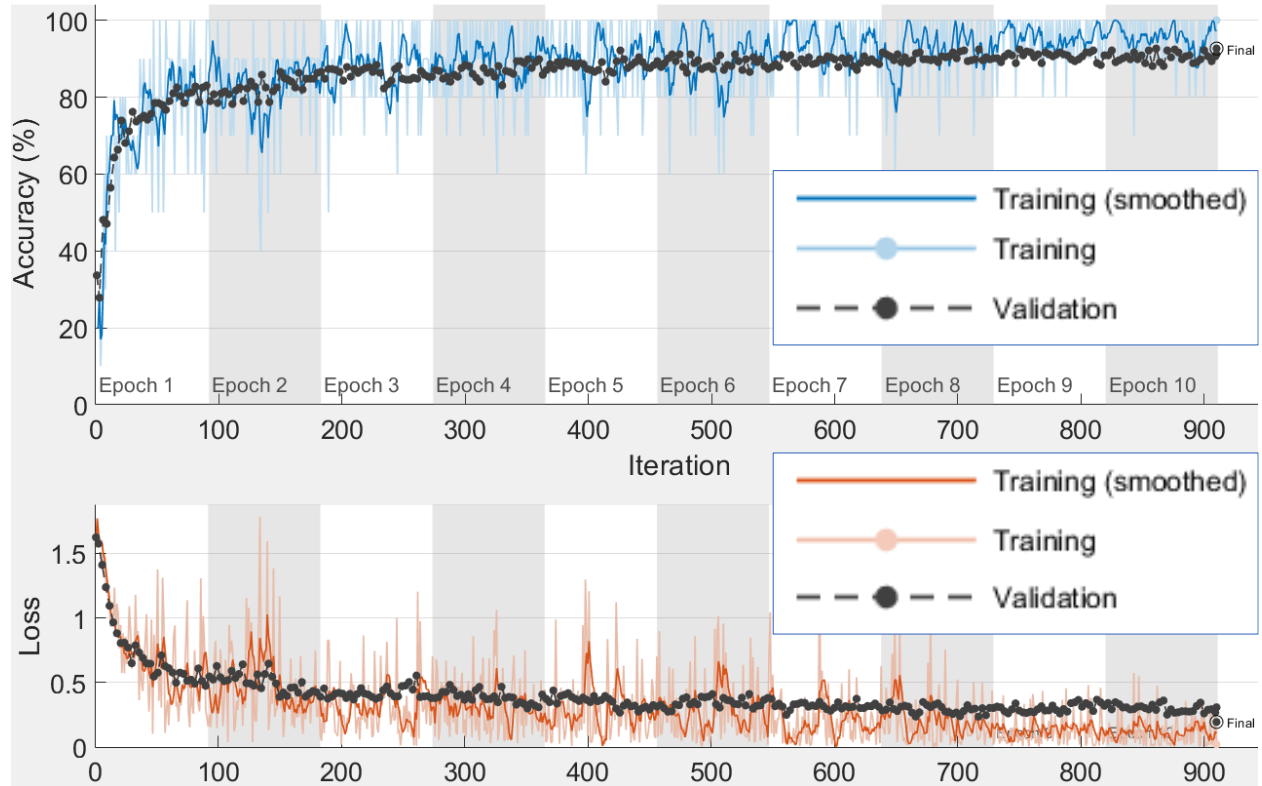


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808



809

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 811 mean average of 93.4% (top), the same parameters are shared by the loss function evaluation  
 812 with a final value of ~0.2 (bottom).

813

**Confusion Matrix**

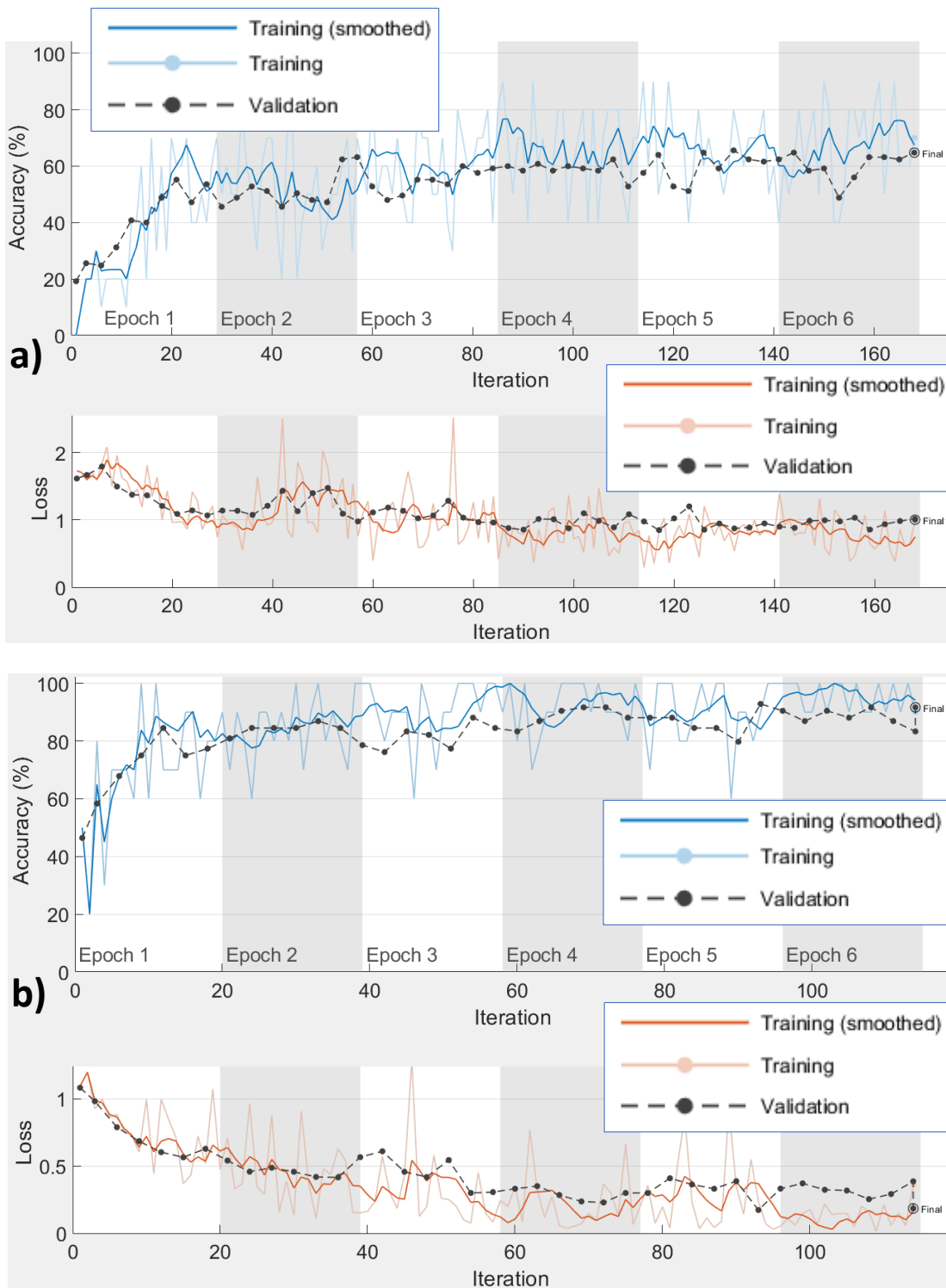
<b>Output Class</b>	AG	65 16.5%	0 0.0%	2 0.5%	1 0.3%	0 0.0%	95.6% 4.4%
	CC	0 0.0%	76 19.2%	0 0.0%	1 0.3%	0 0.0%	98.7% 1.3%
	GR	1 0.3%	0 0.0%	75 19.0%	0 0.0%	0 0.0%	98.7% 1.3%
	PC	13 3.3%	1 0.3%	0 0.0%	75 19.0%	1 0.3%	83.3% 16.7%
	SP	0 0.0%	2 0.5%	2 0.5%	2 0.5%	78 19.7%	92.9% 7.1%
			82.3% 17.7%	96.2% 3.8%	94.9% 5.1%	94.9% 5.1%	98.7% 1.3%
		AG	CC	GR	PC	SP	
		<b>Target Class</b>					

814

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 816 left axis is what the network labeled the input data as, and the bottom axis is what the input data  
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 818 of total immediately below. Green text represents a correct classification, while the red  
 819 percentage is the misclassification of the network. The overall network accuracy is shown in the  
 820 bottom right corner.

821

822

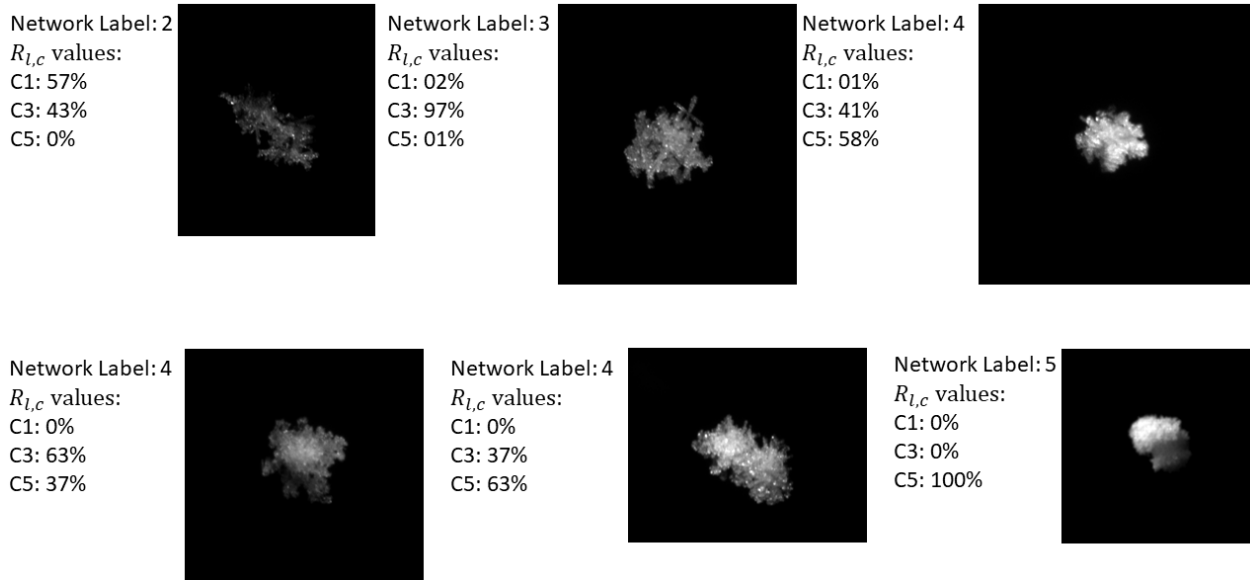


823

824

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 826 discrete riming degree values [1,5] described in Table 1; (b) A separate network was trained  
 827 using the same image data, only removing the images comprising classes 2 and 4.

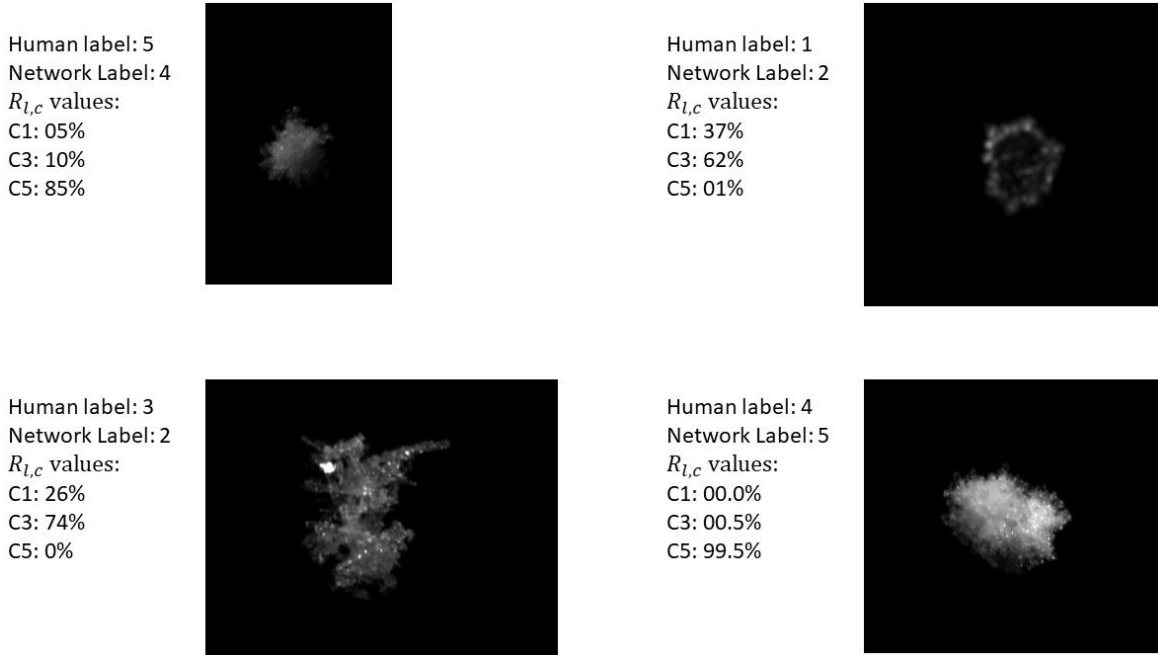
828



829

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833



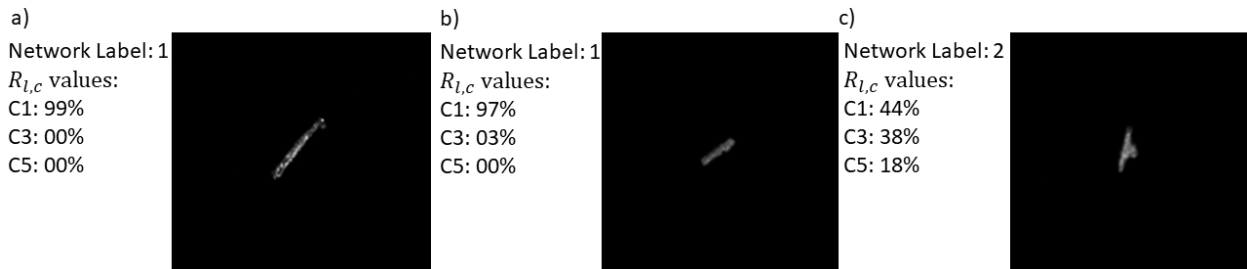
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