

LARGE-SCALE ATMOSPHERIC DYNAMICS
ATS704
Fall 2013

Course Description: Potential vorticity concepts; quasi-geostrophic and semi-geostrophic equations; Rossby waves; barotropic, and baroclinic instability; frontogenesis; Madden-Julian oscillation; tropical cyclones; wave-mean flow interaction; theory of available potential energy and available energy; geophysical turbulence.

Prerequisites: ATS602.

There is no required textbook. Reading material is from the journal literature listed below.

Student learning objectives: To obtain a research-level understanding of problems in large-scale geophysical fluid dynamics, especially those related to current research in weather prediction and climate modeling.

Course Syllabus

1. The Potential Vorticity Conservation Principle
 - 1.1 Ertel's Derivation of the PV Principle (Ertel 1942)
 - 1.2 Conservation and Impermeability Theorems for PV (Haynes and McIntyre 1987, 1990)
 - 1.3 Review of Potential Vorticity Concepts (Hoskins et al. 1985)
 - 1.4 Particle Relabeling Symmetry and Ertel's Theorem (Salmon 1982, 1998)
2. Midlatitude Dynamics
 - 2.1 Baroclinic Instability and the Theory of Extratropical Cyclones (Bretherton 1966a,b, Hoskins 1990)
 - 2.2 Surface and Upper Level Frontogenesis (Hoskins and Bretherton 1972, Fulton and Schubert 1991)
 - 2.3 Semigeostrophic Theory on the f -Plane (Hoskins 1975, Hoskins and Draghici 1977, Hoskins and West 1979, Davies, Schär and Wernli 1991, Schär and Wernli 1993)
 - 2.4 Semigeostrophic Theory on the β -Plane and Hemisphere (Magnusdottir and Schubert 1990, 1991)
 - 2.5 Primitive Equation Models in Isentropic Coordinates (Hsu and Arakawa 1990)
 - 2.6 Baroclinic Life Cycles (Thorncroft et al. 1993, Hartmann and Zuercher 1998)
 - 2.7 Storm Tracks (Hoskins and Hodges 2002, 2005)
 - 2.8 Perspectives on Blocking (Pelly and Hoskins 2003, Berrisford et al. 2007, Tyrlis and Hoskins 2008a, 2008b)
 - 2.9 Quasi-Geostrophic Theory on the Sphere (Mak 1991, Verkley 2009, Schubert et al. 2009)
 - 2.10 Two-Dimensional Turbulence and Predictability (Lee 1951, Fjortoft 1953, Lorenz 1963)
3. Stratospheric Dynamics
 - 3.1 The Overworld, Middleworld and Underworld (Hoskins 1991)
 - 3.2 Stratospheric-Tropospheric Exchange (Danielsen 1968, Holton et al. 1995)
 - 3.3 Breaking Rossby Waves in the Stratosphere (Juckes 1989, Waugh and Plumb 1994, Norton 1994)
 - 3.4 Vertical Propagation of Rossby Waves (Charney and Drazin 1961, Matsuno 1970)
 - 3.5 Sudden Stratospheric Warming (Matsuno 1971)
 - 3.6 Effective diffusivity as a diagnostic of atmospheric transport (Nakamura 1996, 2001, 2004, Haynes and Shuckburgh 2000a,b)
4. Tropical Dynamics

- 4.1 The Intertropical Convergence Zone and the Hadley Circulation in the Climatological Mean (Schneider and Lindzen 1977, Held and Hou 1980, Lindzen and Hou 1988, Philander et al. 1996)
- 4.2 The Intertropical Convergence Zone and the Hadley Circulation on Synoptic Time Scales (Hack et al. 1989, Hack and Schubert 1990, Schubert et al. 1991)
- 4.3 The Shallow Hadley Circulation (Zhang et al. 2004, 2008, Nolan et al. 2007, 2010, Gonzalez and Mora 2013)
- 4.4 The Moisture Field in the Tropics (Cau et al. 2007)
- 4.5 Barotropic-Baroclinic Instability and Easterly Waves (Thorncroft and Hoskins 1994a,b, Nieto Ferreira and Schubert 1997)
- 4.6 Laplace's Tidal Equations and Equatorial β -Plane Theory (Matsuno 1966, Longuet-Higgins 1968)
- 4.7 Longwave Theory and the Walker Circulation (Gill 1980, Heckley and Gill 1984, Gill and Phillips 1986, Phillips and Gill 1987)
- 4.8 The MJO (Madden and Julian 1994, Majda and Klein 2003, Schubert and Masarik 2006)
- 4.9 Improvement of the Longwave Approximation (Ripa 1994, Schubert et al. 2009)
- 4.10 Monsoons and the Dynamics of Deserts (Rodwell and Hoskins 1995, 1996)
- 4.11 Subtropical Anticyclones and Summer Monsoons (Rodwell and Hoskins 1995, 1996, 2001)
- 4.12 The Simplest Theory of Tropical Cyclones (Ooyama 1969)
- 4.13 Full Physics Tropical Cyclone Models (Yamasaki 1983)
- 4.14 A Thermodynamic and Dynamic Foundation for Modeling the Moist Atmosphere (Ooyama 1990, 2001)
- 4.15 The Potential Vorticity Principle for a Moist Atmosphere (Schubert et al. 2001)
- 4.16 PV Mixing in Hurricanes (Schubert et al. 1999, Montgomery et al. 2002, Hendricks and Schubert 2010)
- 4.17 Vortex Rossby Wave Theory (Montgomery and Kallenbach 1997)
- 4.18 Interaction of Tropical-Cyclone Scale Vortices (Lander and Holland 1993, Ritchie and Holland 1993, Holland and Dietachmayer 1993, Prieto et al. 2003)
- 4.19 Scale Interactions in the Tropics (Holland 1995, Simpson et al. 1997, Ritchie and Holland 1999)
- 4.20 MPI Theory (Emanuel 1988, Holland 1997, Persing and Montgomery 2003)
- 4.21 Hurricane Concentric Eyewalls, Eyewall Cycles, and Moats (Willoughby et al. 1982, Willoughby 1990, Kuo et al. 2004, Rozoff et al. 2005, Weiss 1991, Hua and Klein 1998, Abarca and Corbosiero 2011)
- 4.22 The Boundary Layer of a Hurricane (Eliassen 1971, Eliassen and Lystad 1977, Smith 1968, 1980, 2003, Montgomery et al. 2001, Smith and Montgomery 2008, Smith and Vogl 2008, Kepert 2001, 2010a, 2010b, Kepert and Wang 2001, Williams et al. 2013)

5. Hamiltonian Fluid Dynamics (Salmon 1998, Chapter 7)
 - 5.1 Variational Principles in Continuum Mechanics (Seliger and Whitham 1968)
 - 5.2 Practical Use of Hamilton's Principle to Derive Filtered Models (Salmon 1983)
 - 5.3 New Equations for Nearly Geostrophic Flow (Salmon 1985)
 - 5.4 Review of Hamiltonian Fluid Mechanics (Salmon 1988a)
 - 5.5 Semigeostrophic Theory as a Dirac-Bracket Projection (Salmon 1988b)
 - 5.6 Planetary Semigeostrophic Theory (Shutts 1989)
 - 5.7 Non-hydrostatic Filtered Model (Miller and White 1984, White 1989, Salmon and Smith 1994)
 - 5.8 Poisson-bracket approach to the construction of algorithms for the shallow-water equations (Salmon 2004, 2005, 2009)

6. Wave-Mean Flow Interaction
 - 6.1 The Eliassen-Palm Theorem (Eliassen and Palm 1961)
 - 6.2 The Non-Acceleration (Charney-Drazin) Theorem (Charney and Drazin 1961)

- 6.3 The Transformed Eulerian Mean (TEM) Formulation, the Eliassen-Palm (EP) Flux, and the Generalized Eliassen-Palm Relation and Charney-Drazin Theorem (Andrews and McIntyre 1976a,b, 1978a)
- 6.4 The Generalized Lagrangian Mean (GLM) Formulation of Wave-Mean Flow Interaction (Andrews and McIntyre 1978b,c)
- 6.5 Casimir Invariants and the Construction of Two General Wave-Activity Relations: Pseudomomentum and Pseudoenergy (Haynes 1988)
- 6.6 The EP Flux as a Diagnostic of Wave Propagation in the Meridional Plane (Edmon et al. 1980)
- 6.7 On the Interpretation of the EP Flux Divergence (Andrews 1983)
- 6.8 Isentropic Coordinate Version of the Charney-Drazin Theorem (Andrews 1983, Tung 1986)
- 6.9 Available Potential Energy as the Non-Kinetic Part of the Pseudoenergy (Holliday and McIntyre 1981, Andrews 1981, Shepherd 1993)
- 6.10 Review of Wave-Mean Flow Interaction (Grimshaw 1984)
- 6.11 The “Downward Control” Principle and Stratosphere-Troposphere Exchange (Haynes et al. 1991)
- 6.12 The Quasi-biennial Oscillation (Baldwin et al. 2001)
- 6.13 Summary of Applications to the Stratosphere (McIntyre 1992)
- 6.14 A formulation of a phase-independent wave-activity flux for stationary and migratory quasi-geostrophic eddies on a zonally varying basic flow (Takaya and Nakamura 2001)

- 7. Nonlinear Stability Theory
 - 7.1 Fundamental Theory (Arnol'd 1966, 1969)
 - 7.2 Review of the Method (Holm et al. 1985, Abarbanel et al. 1986)
 - 7.3 Fundamental Geophysical Theory (Andrews 1983, McIntyre and Shepherd 1987, Swaters 1986)
 - 7.4 Nonlinear Saturation Bounds (Shepherd 1988)
 - 7.5 Symplectic Approach (Shepherd 1993)
 - 7.6 Extremal States of Hamiltonian Dynamical Systems (Vallis, Carnevale and Young 1989, Shepherd 1990)

- 8. Theory of Available Potential Energy and Available Energy
 - 8.1 Lorenz's Theory (Lorenz 1955, 1960)
 - 8.2 Andrews' Theory (Andrews 1981, 2006)
 - 8.3 Shepherd's Approach (Shepherd 1993)
 - 8.4 Generalization to a Moist Atmosphere (Lorenz 1978, 1979, Randall and Wang 1992)

- 9. Turbulence
 - 9.1 Kolmogorov's Theory
 - 9.2 Two-dimensional Turbulence (Kraichnan 1967, Batchelor 1969)
 - 9.3 Geostrophic Turbulence (Sadourny 1985; Salmon 1998, Chapter 6 and references therein)
 - 9.4 Effects of the Earth's Sphericity (Rhines 1975, Vallis and Maltrud 1993, Huang and Robinson 1998)
 - 9.5 Numerical Simulations of Geophysical Turbulence (McWilliams 1984)
 - 9.6 Zonal Jets (Cho and Polvani 1996a,b, Theiss 2004, Showman 2007, Scott and Polvani 2007, 2008)
 - 9.7 Numerical Simulations of Shallow Water Turbulence (Polvani et al. 1994)
 - 9.8 Spontaneous Radiation of Inertia-Gravity Waves (Ford et al. 2000, Schechter and Montgomery 2005, Hendricks et al. 2010)

- 10. Ocean Circulation Theory (Pedlosky 1997)
 - 10.1 The Wind-Driven Circulation
 - 10.2 The Ventilated Thermocline
 - 10.3 The Equatorial Undercurrent (EUC)

10.4 The Antarctic Circumpolar Current (ACC)

10.5 The Abyssal Circulation

The course will not cover all the above topics, but only selected topics that depend on student interest. There will be no exams. Grades will be based on oral presentations and the ppt file that is prepared for the audience.

REFERENCES

- Abarbanel, H. D. I., D. D. Holm, J. E. Marsden and T. S. Ratiu, 1986: Nonlinear stability analysis of stratified fluid equilibria. *Philos. Trans. R. Soc. London Ser. A*, **318**, 349–409.
- Abarca, S. F., and K. L. Corbosiero, 2011: Secondary eyewall formation in WRF simulations of Hurricanes Rita and Katrina (2005). *Geophys. Res. Lett.*, **38**, L07802.
- Andrews, D. G., 1981: A note on potential energy density in a stratified compressible fluid. *J. Fluid Mech.*, **107**, 227–236.
- Andrews, D. G., 1983: A conservation law for small-amplitude quasi-geostrophic disturbances on a zonally asymmetric basic flow. *J. Atmos. Sci.*, **40**, 85–90.
- Andrews, D. G., 2006: On the available energy density for axisymmetric motions of a compressible stratified fluid. *J. Fluid Mech.*, **569**, 481–492.
- Andrews, D. G., and M. E. McIntyre, 1976a: Planetary waves in horizontal and vertical shear: The generalized Eliassen-Palm relation and the mean zonal acceleration. *J. Atmos. Sci.*, **33**, 2031–2048.
- Andrews, D. G., and M. E. McIntyre, 1976b: Planetary waves in horizontal and vertical shear: asymptotic theory for equatorial waves in weak shear. *J. Atmos. Sci.*, **33**, 2049–2053.
- Andrews, D. G., and M. E. McIntyre, 1978a: Generalized Eliassen-Palm and Charney-Drazin theorems for waves on axisymmetric mean flows in compressible atmospheres. *J. Atmos. Sci.*, **35**, 175–185.
- Andrews, D. G., and M. E. McIntyre, 1978b: An exact theory of nonlinear waves on a Lagrangian-mean flow. *J. Fluid Mech.*, **89**, 609–646.
- Andrews, D. G., and M. E. McIntyre, 1978c: On wave-action and its relatives. *J. Fluid Mech.*, **89**, 647–664.
- Arnol'd, V. I., 1966: On an a priori estimate in the theory of hydrodynamical stability. *Am. Math. Soc. Transl. Ser. 2*, **79**, 267–269.
- Arnol'd, V. I., 1969: The Hamiltonian nature of the Euler equations in the dynamics of a rigid body and of a perfect fluid. *Usp. Mat. Nauk.*, **24**, 225–226 (In Russian).
- Batchelor, G. K., 1969: Computation of the energy spectrum in homogeneous two-dimensional turbulence. *Phys. Fluids Supplement II*, 233.
- Berrisford, P., B. J. Hoskins, and E. Tyrlis, 2007: Blocking and Rossby Wave breaking on the dynamical tropopause in the southern hemisphere. *J. Atmos. Sci.*, **64**, 2881–2898.
- Bretherton, F. P., 1966a: Critical layer instability in baroclinic flows. *Quart. J. Roy. Meteor. Soc.*, **92**, 325–334.

- Bretherton, F. P., 1966b: Baroclinic instability and the short wavelength cutoff in terms of potential vorticity. *Quart. J. Roy. Meteor. Soc.*, **92**, 335–345.
- Bretherton, F. P., 1970: A note on Hamilton's principle for perfect fluids. *J. Fluid Mech.*, **44**, 19–31.
- Cau, P., J. Methven, and B. J. Hoskins, 2007: Origins of dry air in the tropics and subtropics. *J. Climate*, **20**, 2745–2759.
- Charney, J. G., and P. G. Drazin, 1961: Propagation of planetary-scale disturbances from the lower into the upper atmosphere. *J. Geophys. Res.*, **66**, 83–109.
- Cho, J. Y.-K., and L. M. Polvani, 1996a: The emergence of jets and vortices in freely-evolving shallow-water turbulence on a sphere. *Phys. Fluids*, **8**, 1531–1552.
- Cho, J. Y.-K., and L. M. Polvani, 1996b: The morphogenesis of bands and zonal winds in the atmospheres on the giant outer planets. *Science*, **273**, 335–337.
- Davies, H. C., and Ch. Schä r, and H. Wernli, 1991: The palette of fronts and cyclones within a baroclinic wave development. *J. Atmos. Sci.*, **48**, 1666–1689.
- Danielsen, E. F., 1968: Stratospheric-tropospheric exchange based on radioactivity, ozone and potential vorticity. *J. Atmos. Sci.*, **25**, 502–518.
- Edmon, H. J., B. J. Hoskins and M. E. McIntyre, 1980: Eliassen-Palm cross-sections for the troposphere. *J. Atmos. Sci.*, **37**, 2600–2616.
- Eliassen, A., 1971: On the Ekman layer in a circular vortex. *J. Meteor. Soc. Japan*, **49**, 784–789.
- Eliassen, A., and M. Lystad, 1977: The Ekman layer of a circular vortex: A numerical and theoretical study. *Geophys. Norv.*, **31**, 1–16.
- Eliassen, A., and E. Palm, 1961: On the transfer of energy in stationary mountain waves. *Geofys. Publ.*, **22**, 1–23.
- Emanuel, K. A., 1988: The maximum intensity of hurricanes. *J. Atmos. Sci.*, **45**, 1143–1155.
- Ertel, H., 1942: Ein neuer hydrodynamischer Wirbelsatz. *Meteorol. Z.*, **59**, 271–281.
- Fjortoft, R., 1953: On the changes in the spectral distribution of kinetic energy for two-dimensional nondivergent flow. *Tellus*, **5**, 225–230.
- Fulton, S. R., and W. H. Schubert, 1991: Surface frontogenesis in isentropic coordinates. *J. Atmos. Sci.*, **48**, 2534–2541.
- Gill, A. E., 1975: Models of equatorial currents. *Numerical Models of Ocean Circulation*, National Academy of Sciences, Washington D. C., 181–203.
- Gill, A. E., 1980: Some simple solutions for heat-induced tropical circulation. *Quart. J. Roy. Meteor. Soc.*, **106**, 447–462.
- Gill, A. E., 1985: Elements of coupled ocean-atmosphere models for the tropics. *Coupled Ocean-Atmosphere Models*, Edited by J. Nihoul, Elsevier Oceanography Services, **40**, 303–327.

- Gill, A. E., and P. J. Phlips, 1986: Nonlinear effects on heat-induced circulations of the tropical atmosphere. *Quart. J. Roy. Meteor. Soc.*, **112**, 69–91.
- Hack, J. J., and W. H. Schubert, 1990: Some dynamical properties of idealized thermally-forced meridional circulations in the tropics. *Meteorol. Atmos. Phys.*, **44**, 101–117.
- Hack, J. J., W. H. Schubert, D. E. Stevens, and H.-C. Kuo, 1989: Response of the Hadley circulation to convective forcing in the ITCZ. *J. Atmos. Sci.*, **46**, 2957–2973.
- Hartmann, D. L., and P. Zuercher, 1998: Response of baroclinic life cycles to barotropic shear. *J. Atmos. Sci.*, **55**, 297–313.
- Haynes, P. H., 1988: Forced, dissipative generalizations of finite-amplitude wave-activity conservation relations for zonal and non-zonal basic flows. *J. Atmos. Sci.*, **45**, 2352–2362.
- Haynes, P. H., and M. E. McIntyre, 1987: On the evolution of vorticity and potential vorticity in the presence of diabatic heating and frictional or other forces. *J. Atmos. Sci.*, **44**, 828–841.
- Haynes, P. H., and M. E. McIntyre, 1990: On the conservation and impermeability theorems for potential vorticity. *J. Atmos. Sci.*, **47**, 2021–2031.
- Haynes, P. H., C. J. Marks, M. E. McIntyre, T. G. Shepherd and K. P. Shine, 1991: On the “downward control” of extratropical diabatic circulations by eddy-induced mean zonal forces. *J. Atmos. Sci.*, **48**, 651–678.
- Haynes, P., and E. Shuckburgh, 2000a: Effective diffusivity as a diagnostic of atmospheric transport. 1. Stratosphere. *J. Geophys. Res.*, **105**, No. D18, 22,777–22,794.
- Haynes, P., and E. Shuckburgh, 2000b: Effective diffusivity as a diagnostic of atmospheric transport. 2. Troposphere and lower stratosphere. *J. Geophys. Res.*, **105**, No. D18, 22,795–22,810.
- Heckley, W. A., and A. E. Gill, 1984: Some simple analytical solutions to the problem of forced equatorial long waves. *Quart. J. Roy. Meteor. Soc.*, **110**, 2103–217.
- Held, I. M., and A. Y. Hou, 1980: Nonlinear axially symmetric circulations in a nearly inviscid atmosphere. *J. Atmos. Sci.*, **37**, 515–533.
- Hendricks, E. A., and W. H. Schubert, 2010: Adiabatic rearrangement of hollow PV towers. *J. Adv. Model. Earth Syst.*, **2**, in press.
- Hendricks, E. A., W. H. Schubert, S. R. Fulton, and B. D. McNoldy, 2010: Spontaneous-adjustment emission of inertia-gravity waves by unsteady vortical motion in the hurricane core. *Quart. J. Roy. Meteor. Soc.*, **136**, 537–548.
- Holland, G. J., 1995: Scale interaction in the Western Pacific monsoon. *Meteorol. Atmos. Phys.*, **56**, 57–79.
- Holland, G. J., 1997: The maximum potential intensity of tropical cyclones. *J. Atmos. Sci.*, **54**, 2519–2541.
- Holland, G. J., and G. S. Dietachmayer, 1993: On the interaction of tropical-cyclone scale vortices. III: Continuous barotropic vortices. *Quart. J. Roy. Meteor. Soc.*, **119**, 1381–1398.

- Holliday, D., and M. E. McIntyre, 1981: On potential energy density in an incompressible, stratified fluid. *J. Fluid Mech.*, **107**, 221–225.
- Holm, D. D., J. E. Marsden, T. Ratiu and A. Weinstein, 1985: Nonlinear stability of fluid and plasma equilibria. *Phys. Rep.*, **123**, 1–116.
- Holton, J. R., P. Haynes, M. E. McIntyre, A. R. Douglass, R. Rood, L. Pfister, 1995: Stratosphere-troposphere exchange. *Rev. Geophys.*, **33**, 403–439.
- Hoskins, B. J., 1975: The geostrophic momentum approximation and the semi-geostrophic equations. *J. Atmos. Sci.*, **32**, 233–242.
- Hoskins, B. J., 1990: Theory of extratropical cyclones. *Extratropical Cyclones: The Erik Palmen Memorial Volume*, American Meteorological Society, 262 pages.
- Hoskins, B. J., 1991: Towards a PV- θ view of the general circulation. *Tellus*, **43AB**, 27–35.
- Hoskins, B. J., and F. P. Bretherton, 1972: Atmospheric frontogenesis models: mathematical formulation and solution. *J. Atmos. Sci.*, **29**, 11–37.
- Hoskins, B. J., and I. Draghici, 1977: The forcing of ageostrophic motion according to the semi-geostrophic equations and in an isentropic coordinate model. *J. Atmos. Sci.*, **34**, 1859–1867.
- Hoskins, B. J., and K. I. Hodges, 2002: New perspectives on the northern hemisphere winter storm tracks. *J. Atmos. Sci.*, **59**, 1041–1061.
- Hoskins, B. J., and K. I. Hodges, 2005: A new perspective on southern hemisphere storm tracks. *J. Climate*, **18**, 4108–4129.
- Hoskins, B. J., and N. V. West, 1979: Baroclinic waves and frontogenesis. Part II: Uniform potential vorticity jet flows—cold and warm fronts. *J. Atmos. Sci.*, **36**, 1663–1680.
- Hoskins, B. J., M. E. McIntyre and A. W. Robertson, 1985: On the use and significance of isentropic potential vorticity maps. *Quart. J. R. Met. Soc.*, **111**, 877–946.
- Hsu, and A. Arakawa, 1990: Numerical modeling of the atmosphere with an isentropic vertical coordinate. *Mon. Wea. Rev.*, **118**, 1933–1959.
- Hua, B. L., and P. Klein, 1998: An exact criterion for the stirring properties of nearly two-dimensional turbulence. *Physica D*, **113**, 98–110.
- Huang, H.-P., and W. A. Robinson, 1998: Two-dimensional turbulence and persistent zonal jets in a global barotropic model. *J. Atmos. Sci.*, **55**, 611–632.
- Juckes, M., 1989: A shallow water model of the winter stratosphere. *J. Atmos. Sci.*, **46**, 2934–2955.
- Kepert, J. D., 2001: The dynamics of boundary layer jets within the tropical cyclone core. Part I: Linear theory. *J. Atmos. Sci.*, **58**, 2469–2484.
- Kepert, J. D., 2010a: Slab and height-resolving models of the tropical cyclone boundary layer. Part I: Comparing the simulations. *Quart. J. R. Met. Soc.*, **136**, 1686–1699.

- Kepert, J. D., 2010b: Slab and height-resolving models of the tropical cyclone boundary layer. Part II: Why the simulations differ. *Quart. J. R. Met. Soc.*, **136**, 1700–1711.
- Kepert, J. D., and Y. Wang, 2001: The dynamics of boundary layer jets within the tropical cyclone core. Part II: Nonlinear enhancement. *J. Atmos. Sci.*, **58**, 2485–2501.
- Kraichnan, R. H., 1967: Inertial ranges in two-dimensional turbulence. *Phys. Fluids*, **10**, 1417–1423.
- Kuo, H.-C., L.-Y. Lin, C.-P. Chang, and R. T. Williams, 2004: The formation of concentric vorticity structures in typhoons. *J. Atmos. Sci.*, **61**, 2722–2734.
- Lander, M., and G. J. Holland, 1993: On the interaction of tropical-cyclone scale vortices. I: Observations. *Quart. J. Roy. Meteor. Soc.*, **119**, 1347–1361.
- Lee, T. D., 1951: Difference between turbulence in a two-dimensional fluid and in a three-dimensional fluid. *J. Applied Phys.*, **22**, 524.
- Lin, C. C., 1963: Hydrodynamics of helium II. *Proc. Int. Sch. Phys. XXI*, 93–146. Academic Press, New York.
- Lindzen, R. S., and A. Y. Hou, 1988: Hadley circulation for zonally averaged heating centered off the equator. *J. Atmos. Sci.*, **45**, 2416–2427.
- Longuet-Higgins, M. S., 1968: The eigenfunctions of Laplace's tidal equations over the sphere. *Phil. Trans. Roy. Soc. London*, **A262**, 511–607.
- Lorenz, E. N., 1955: Available energy and the maintenance of the general circulation. *Tellus*, **7**, 157–167.
- Lorenz, E. N., 1960: Energy and numerical weather prediction. *Tellus*, **12**, 364–373.
- Lorenz, E. N., 1978: Available energy and the maintenance of a moist circulation. *Tellus*, **30**, 15–31.
- Lorenz, E. N., 1979: Numerical evaluation of moist available energy. *Tellus*, **31**, 230–235.
- Madden, R. A., and Julian, P. R., 1994: Observations of the 40–50-day tropical oscillation—A review. *Mon. Wea. Rev.*, **122**, 814–837.
- Majda, A. J., and Klein, R., 2003: Systematic multiscale models for the tropics. *J. Atmos. Sci.*, **60**, 393–408.
- Magnusdottir, G., and W. H. Schubert, 1990: On the generalization of semigeostrophic theory to the β -plane. *J. Atmos. Sci.*, **47**, 1714–1720.
- Magnusdottir, G., and W. H. Schubert, 1991: Semigeostrophic theory on the hemisphere. *J. Atmos. Sci.*, **48**, 1449–1456.
- Mak, M.-K., 1991: Influences of the earth's sphericity in quasi-geostrophic theory. *J. Meteor. Soc. Japan*, **69**, 497–510.
- Matsuno, T., 1970: Vertical propagation of stationary planetary waves in the winter northern hemisphere. *J. Atmos. Sci.*, **27**, 831–883.

- Matsuno, T., 1971: A dynamical model of the stratospheric sudden warming. *J. Atmos. Sci.*, **28**, 1479–1494.
- McIntyre, M. E., 1992: Atmospheric dynamics: Some fundamentals, with observational implications. *Proc. Int. School Phys. “Enrico Fermi” CXV Course, The Use of EOS for Studies of Atmospheric Physics*, eds. J. C. Gille and G. Visconti, North-Holland, 313–386.
- McIntyre, M. E., and T. G. Shepherd, 1987: An exact local conservation theorem for finite-amplitude disturbances to nonparallel shear flows, with remarks on Hamiltonian structure and on Arnold’s stability theorems. *J. Fluid Mech.*, **181**, 527–565.
- McWilliams, J. C., 1984: The emergence of isolated coherent vortices in turbulent flow. *J. Fluid Mech.*, **146**, 21–43.
- Miller, M. J., and A. A. White, 1984: On the non-hydrostatic equations in pressure and sigma coordinates. *Quart. J. R. Met. Soc.*, **110**, 515–533.
- Montgomery, M. T., V. A. Vladimirov, and P. V. Denissenko, 2002: An experimental study on hurricane mesovortices. *J. Fluid Mech.*, **471**, 1–32.
- Montgomery, M. T., and R. J. Kallenbach, 1997: A theory of vortex Rossby waves and its application to spiral bands and intensity changes in hurricanes. *Quart. J. R. Met. Soc.*, **123**, 435–465.
- Montgomery, M. T., H. D. Snell, and Z. Yang, 2001: Axisymmetric spindown dynamics of hurricane-like vortices. *J. Atmos. Sci.*, **58**, 421–435.
- Nakamura, N., 1996: Two-dimensional mixing, edge formation, and permeability diagnosed in an area coordinate. *J. Atmos. Sci.*, **53**, 1524–1537.
- Nakamura, N., 2001: A new look at eddy diffusivity as a mixing diagnostic. *J. Atmos. Sci.*, **58**, 3685–3701.
- Nakamura, N., 2004: Quantifying asymmetric wave breaking and two-way transport. *J. Atmos. Sci.*, **61**, 2735–2748.
- Nieto Ferreira, R., and W. H. Schubert, 1997: Barotropic aspects of ITCZ breakdown. *J. Atmos. Sci.*, **54**, 261–285.
- Nolan, D. S., C. Zhang, and S.-H. Chen, 2007: Dynamics of the shallow meridional circulation around Intertropical Convergence Zones. *J. Atmos. Sci.*, **64**, 2262–2285.
- Nolan, D. S., S. W. Powell, C. Zhang, and B. E. Mapes, 2010: Idealized simulations of the Intertropical Convergence Zone and its multilevel flows. *J. Atmos. Sci.*, **64**, 2262–2285.
- Norton, W. A., 1994: Breaking Rossby waves in a model stratosphere diagnosed by a vortex-following coordinate system and a technique for advecting material contours. *J. Atmos. Sci.*, **51**, 654–673.
- Ooyama, K. V., 1969: Numerical simulation of the life cycle of tropical cyclones. *J. Atmos. Sci.*, **26**, 3–40.
- Ooyama, K. V., 1990: A thermodynamic foundation for modeling the moist atmosphere. *J. Atmos. Sci.*, **47**, 2580–2593.

- Ooyama, K. V., 2001: A dynamic and thermodynamic foundation for modeling the moist atmosphere with parameterized microphysics. *J. Atmos. Sci.*, **58**, 2073–2102.
- Pedlosky, J., 1997: Ocean Circulation Theory.
- Pelly, J. L., and B. J. Hoskins, 2003: A new perspective on blocking. *J. Atmos. Sci.*, **60**, 743–755.
- Persing, J., and M. T. Montgomery, 2003: Hurricane superintensity. *J. Atmos. Sci.*, **60**, 2349–2371.
- Philander, S. G. H., D. Gu, D. Halpern, G. Lambert, N., C. Lau, T. Li, and R. C. Pacanowski, 1996: Why the ITCZ is mostly north of the equator. *J. Climate*, **9**, 2958–2972.
- Phlips, P. J., and A. E. Gill, 1987: An analytic model of the heat-induced tropical circulation in the presence of a mean wind. *Quart. J. Roy. Meteor. Soc.*, **113**, 213–236.
- Polvani, L. M., J. C. Mcwilliams, M. Spall, and R. Ford, 1994: The coherent structures of shallow water turbulence: Deformation radius effects, cyclone/anticyclone asymmetry and gravity wave generation. *Chaos*, **4**, 177–186.
- Prieto, R., B. D. McNoldy, S. R. Fulton, and W. H. Schubert, 2003: A classification of binary tropical-cyclone-like vortex interactions. *Mon. Wea. Rev.*, **131**, 2656–2666.
- Randall, D. A., and J. Wang, 1992: The moist available energy of a conditionally unstable atmosphere. *J. Atmos. Sci.*, **49**, 240–255.
- Rhines, P. B., 1975: Waves and turbulence on a beta-plane. *J. Fluid Mech.*, **69**, 417–443.
- Ripa, P., 1994: Horizontal wave propagation in the equatorial waveguide. *J. Fluid Mech.*, **271**, 277–284.
- Ritchie, E. A., and G. J. Holland, 1993: On the interaction of tropical-cyclone scale vortices. II: Interacting vortex patches. *Quart. J. Roy. Meteor. Soc.*, **119**, 1363–1379.
- Ritchie, E. A., and G. J. Holland, 1999: Large-scale patterns associated with tropical cyclogenesis in the Western Pacific. *Mon. Wea. Rev.*, **127**, 2027–2043.
- Rodwell, M. J., and B. J. Hoskins, 1995: A model of the Asian summer monsoon. II: Cross-equatorial flow and PV behaviour. *J. Atmos. Sci.*, **52**, 1341–1356.
- Rodwell, M. J., and B. J. Hoskins, 1996: Monsoons and the dynamics of deserts. *Quart. J. Roy. Meteor. Soc.*, **122**, 1385–1404.
- Rodwell, M. J., and B. J. Hoskins, 2001: Subtropical anticyclones and summer monsoons. *J. Climate*, **14**, 3192–3211.
- Rossby, C-G., 1936: Dynamics of steady ocean currents in the light of experimental fluid dynamics. *Papers in Phys. Oceanog. and Meteor.*, **5**, 1–43.
- Rossby, C-G., and Collaborators, 1937: Isentropic analysis. *Bull. Amer. Meteor. Soc.*, **18**, 201–209.
- Rossby, C-G., 1938: On the mutual adjustment of pressure and velocity distributions in certain simple current systems, II. *J. Mar. Res.*, **5**, 239–263.

- Rossby, C-G., 1940: Planetary flow patterns in the atmosphere. *Quart. J. Roy. Meteor. Soc. (suppl)*, **66**, 68–87.
- Rozoff, C. M., W. H. Schubert, B. D. McNoldy, and J. P. Kossin, 2005: Rapid filamentation zones in intense tropical cyclones. *J. Atmos. Sci.*, **62**, 325–340.
- Sadourny, R., 1985: Quasi-geostrophic turbulence: An introduction. *Proceedings of the International School of Physics, “Enrico Fermi.” Course 88: Turbulence and Predictability in Geophysical Fluid Dynamics and Climate Dynamics*. North-Holland Physics Publishing, 133–158.
- Salmon, R., 1982: Hamilton’s principle and Ertel’s theorem. In *Mathematical Methods in Hydrodynamics and Integrability in Dynamical Systems* (ed. M. Tabor and Y. Treve), Amer. Inst. Phys. Conf. Proc. Vol. **88**, 127–135.
- Salmon, R., 1983: Practical use of Hamilton’s principle. *J. Fluid Mech.*, **132**, 431–444.
- Salmon, R., 1985: New equations for nearly geostrophic flow. *J. Fluid Mech.*, **153**, 461–477.
- Salmon, R., 1988a: Hamiltonian fluid mechanics. *Ann. Rev. Fluid Mech.*, **20**, 225–256.
- Salmon, R., 1988b: Semigeostrophic theory as a Dirac-bracket projection. *J. Fluid Mech.*, **196**, 345–358.
- Salmon, R., 1998: Lectures on Geophysical Fluid Dynamics. Oxford University Press, 378 pp.
- Salmon, R., 2005: A general method for conserving quantities related to potential vorticity in numerical models. *Nonlinearity*, **18**, 1–16.
- Salmon, R., 2009: A shallow water model conserving energy and potential enstrophy in the presence of boundaries. *J. Marine Research*, **67**, 1–36.
- Salmon, R., and L. M. Smith, 1994: Hamiltonian derivation of the nonhydrostatic pressure-coordinate model. *Quart. J. R. Met. Soc.*, **120**, 1409–1413.
- Schär, C., and H. Wernli, 1993: Structure and evolution of an isolated semi-geostrophic cyclone. *Quart. J. R. Met. Soc.*, **119**, 57–90.
- Schneider, E. K., and R. S. Lindzen, 1977: Axially symmetric steady-state models of the basic state for instability and climate studies. Part I: Linearized calculations. *J. Atmos. Sci.*, **34**, 263–279.
- Schubert, W. H., P. E. Ciesielski, D. E. Stevens, and H.-C. Kuo, 1991: Potential vorticity modeling of the ITCZ and the Hadley circulation. *J. Atmos. Sci.*, **48**, 1493–1509.
- Schubert, W. H., S. A. Hausman, M. Garcia, K. V. Ooyama, and H.-C. Kuo, 2001: Potential vorticity in a moist atmosphere. *J. Atmos. Sci.*, **58**, 3148–3157.
- Schubert, W. H., and M. T. Masarik, 2006: Potential vorticity aspects of the MJO. *Dyn. Atmos. Oceans*, **42**, 127–151.
- Schubert, W. H., M. T. Montgomery, R. K. Taft, T. A. Guinn, S. R. Fulton, J. P. Kossin, and J. P. Edwards, 1999: Polygonal eyewalls, asymmetric eye contraction, and potential vorticity mixing in hurricanes. *J. Atmos. Sci.*, **56**, 1197–1223.

- Schubert, W. H., R. K. Taft, and L. G. Silvers, 2009: Shallow water quasi-geostrophic theory on the sphere. *J. Adv. Model. Earth Syst.*, **1**, Art.#2.
- Schubert, W. H., L. G. Silvers, M. T. Masarik, and A. O. Gonzalez, 2009: A filtered model of tropical wave motions. *J. Adv. Model. Earth Syst.*, **1**, Art.#3.
- Scott, R. K., and L. M. Polvani, 2007: Forced-dissipative shallow-water turbulence on the sphere and the atmospheric circulation of the gas planets. *J. Atmos. Sci.*, **64**, 3158–3176.
- Scott, R. K., and L. M. Polvani, 2008: Equatorial superrotation in shallow atmospheres. *Geophys. Res. Lett.*, **35**, L24202.
- Seliger, R. L., and G. B. Whitham, 1968: Variational principles in continuum mechanics. *Proc. R. Soc. Lond.*, **A305**, 1–25.
- Shepherd, T. G., 1988: Rigorous bounds on the nonlinear saturation of instabilities to parallel shear flows. *J. Fluid Mech.*, **196**, 291–322.
- Shepherd, T. G., 1990: A general method for finding extremal states of Hamiltonian dynamical systems, with applications to perfect fluids. *J. Fluid Mech.*, **213**, 573–587.
- Shepherd, T. G., 1990: Symmetries, conservation laws, and Hamiltonian structure in geophysical fluid dynamics. *Advances in Geophysics*, **32**, 287–338.
- Shepherd, T. G., 1993: A unified theory of available potential energy. *Atmos. Ocean*, **31**, 1–26.
- Showman, A. P., 2007: Numerical simulations of forced shallow-water turbulence: Effects of moist convection on the large-scale circulation of Jupiter and Saturn. *J. Atmos. Sci.*, **64**, 3132–3157.
- Shutts, G. J., 1989: Planetary semi-geostrophic equations derived from Hamilton's principle. *J. Fluid Mech.*, **208**, 545–573.
- Simpson, J., E. Ritchie, G. J. Holland, J. Halverson, and S. Stewart, 1997: Mesoscale interactions in tropical cyclone genesis. *Mon. Wea. Rev.*, **125**, 2643–2661.
- Smith, R. K., 1968: The surface boundary layer of a hurricane. *Tellus*, **20**, 473–484.
- Smith, R. K., 1980: Tropical cyclone eye dynamics. *J. Atmos. Sci.*, **37**, 1227–1232.
- Smith, R. K., 2003: A simple model of the hurricane boundary layer. *Quart. J. Roy. Meteor. Soc.*, **129**, 1007–1027.
- Smith, R. K., and M. T. Montgomery, 2008: Balanced boundary layers in hurricane models. *Quart. J. Roy. Meteor. Soc.*, **134**, 1385–1395.
- Smith, R. K., and S. Vogl, 2008: A simple model of the hurricane boundary layer revisited. *Quart. J. Roy. Meteor. Soc.*, **134**, 337–351.
- Swaters, G. E., 1986: A nonlinear stability theorem for baroclinic quasigeostrophic flow. *Phys. Fluids*, **29**, 5–6.
- Takaya, K., and H. Nakamura, 2001: A formulation of a phase-independent wave-activity flux for stationary and migratory quasigeostrophic eddies on a zonally varying basic flow. *J. Atmos. Sci.*, **58**, 608–627.

- Theiss, J., 2004: Equatorward energy cascade, critical latitude, and the predominance of cyclonic vortices in geostrophic turbulence. *J. Phys. Oceanogr.*, **34**, 1663–1678.
- Thorncroft, C. D., and B. J. Hoskins, 1994a: An idealized study of African easterly waves. I: A linear view. *Quart. J. R. Met. Soc.*, **120**, 953–982.
- Thorncroft, C. D., and B. J. Hoskins, 1994b: An idealized study of African easterly waves. II: A nonlinear view. *Quart. J. R. Met. Soc.*, **120**, 983–1015.
- Thorncroft, C. D., B. J. Hoskins, and M. E. McIntyre, 1993: Two paradigms of baroclinic life-cycle behaviour. *Quart. J. R. Met. Soc.*, **119**, 17–55.
- Tung, K. K., 1986: Nongeostrophic theory of zonally averaged circulation. Part I: Formulation. *J. Atmos. Sci.*, **43**, 2600–2618.
- Tyrlis, E., and B. J. Hoskins, 2008a: Aspects of a Northern Hemisphere atmospheric blocking climatology. *J. Atmos. Sci.*, **65**, 1638–1652.
- Tyrlis, E., and B. J. Hoskins, 2008b: The morphology of Northern Hemisphere blocking. *J. Atmos. Sci.*, **65**, 1653–1665.
- Vallis, G. K., G. F. Carnevale and W. R. Young, 1989: Extremal energy properties and construction of stable solutions of the Euler equations. *J. Fluid Mech.*, **207**, 133–152.
- Vallis, G. K., and M. E. Maltrud, 1993: Generation of mean flows and jets on a beta plane and over topography. *J. Phys. Oceanogr.*, **23**, 1346–1362.
- Verkley, W. T. M., 2009: A balanced approximation of the one-layer shallow-water equations on a sphere. *J. Atmos. Sci.*, **66**, 1735–1748.
- Waugh, D. W., and R. A. Plumb, 1994: Contour advection with surgery: A technique for investigating finescale structure in tracer transport. *J. Atmos. Sci.*, **51**, 530–540.
- White, A. A., 1989: An extended version of a nonhydrostatic, pressure coordinate model. *Quart. J. R. Met. Soc.*, **115**, 1243–1251.
- Williams, G. J., R. K. Taft, B. D. McNoldy, and W. H. Schubert, 2013: Shock-like structures in the tropical cyclone boundary layer. *J. Adv. Model. Earth Syst.*, **5**, 1–16.
- Weiss, J., 1991: The dynamics of enstrophy transfer in two-dimensional hydrodynamics. *Physica D*, **48**, 273–294.
- Willoughby, H. E., 1990: Temporal changes of the primary circulation in tropical cyclones. *J. Atmos. Sci.*, **47**, 242–264.
- Willoughby, H. E., J. A. Clos, and M. G. Shoreibah, 1982: Concentric eyewalls, secondary wind maxima, and the evolution of the hurricane vortex. *J. Atmos. Sci.*, **39**, 395–411.
- Yamasaki, M., 1983: A further study of the tropical cyclone without parameterizing the effects of cumulus convection. *Papers Meteor. Geophys.*, **34**, 221–260.
- Zhang, C., M. McGauley, and N. A. Bond, 2004: Shallow meridional circulation in the tropical eastern Pacific. *J. Climate*, **17**, 133–139.
- Zhang, C., D. S. Nolan, C. D. Thorncroft, and H. Nguyen, 2008: Shallow meridional circulations in the tropical atmosphere, *J. Climate*, **21**, 3453–3470.